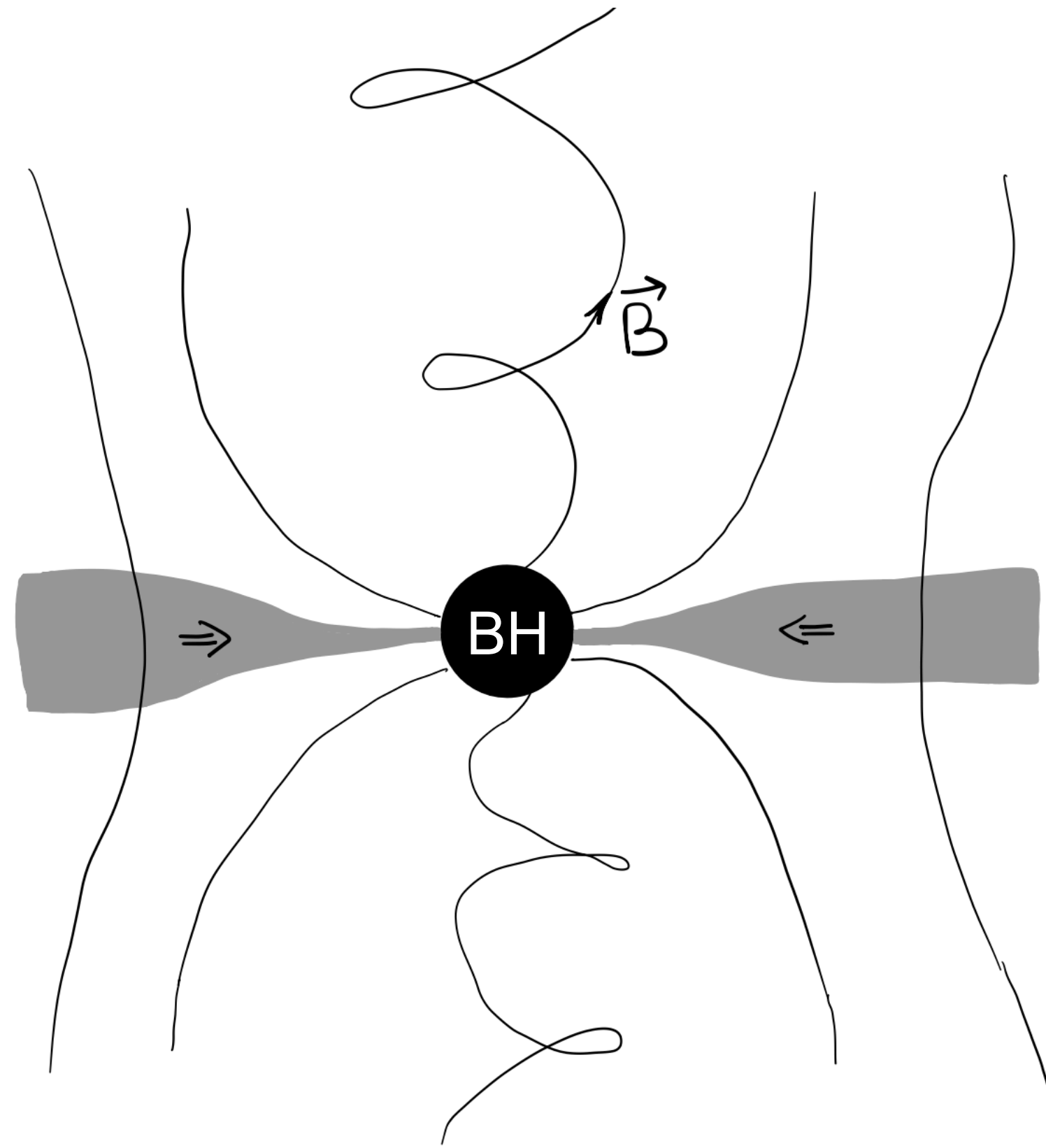


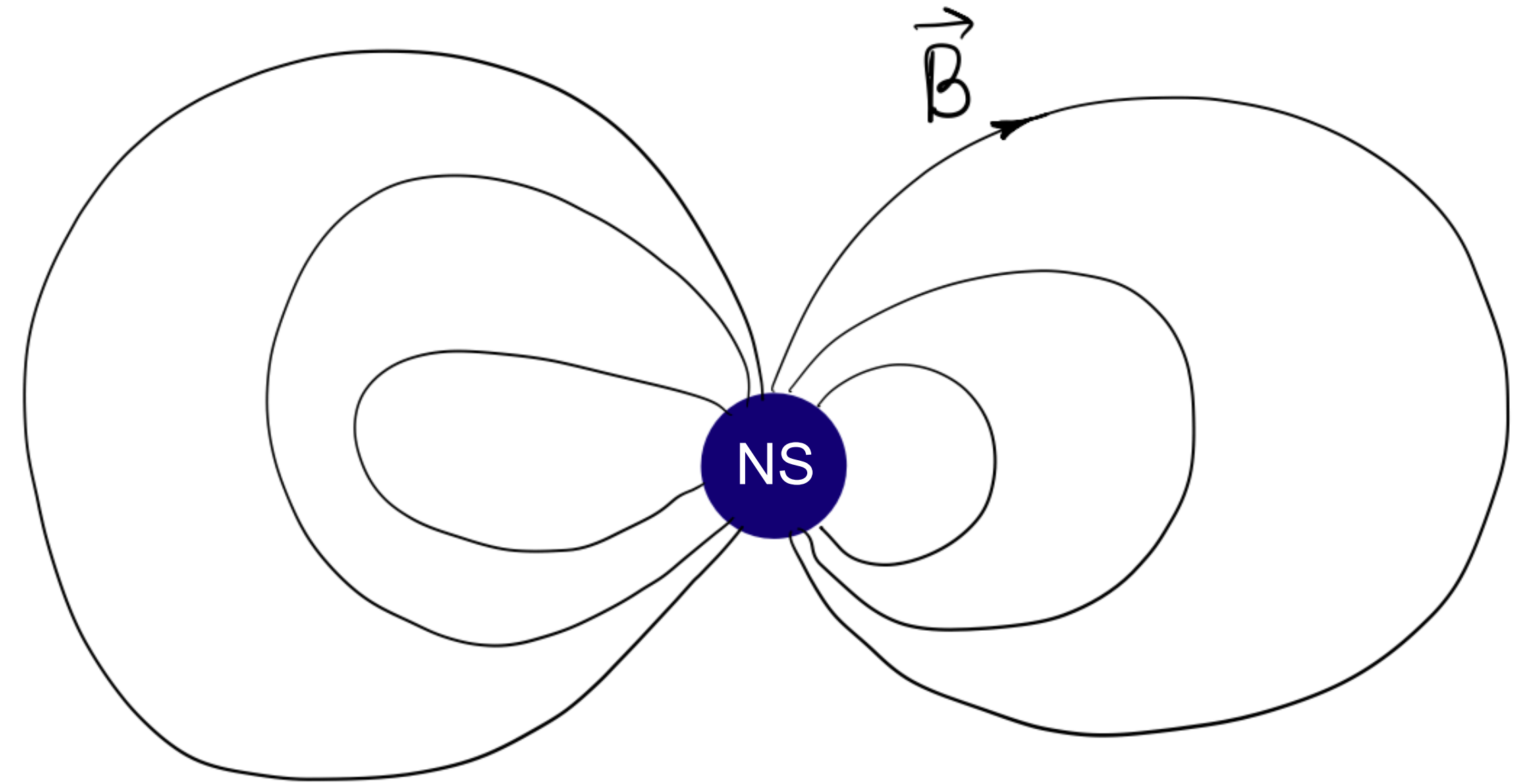
Bursts and relativistic ejecta from magnetars

Andrei Beloborodov
Columbia University

- Quakes
- Nonlinear waves and monster shocks
- Relativistic ejecta
- Bursts (X/ gamma and radio)



Black holes have externally imposed magnetic fields (brought by accretion)



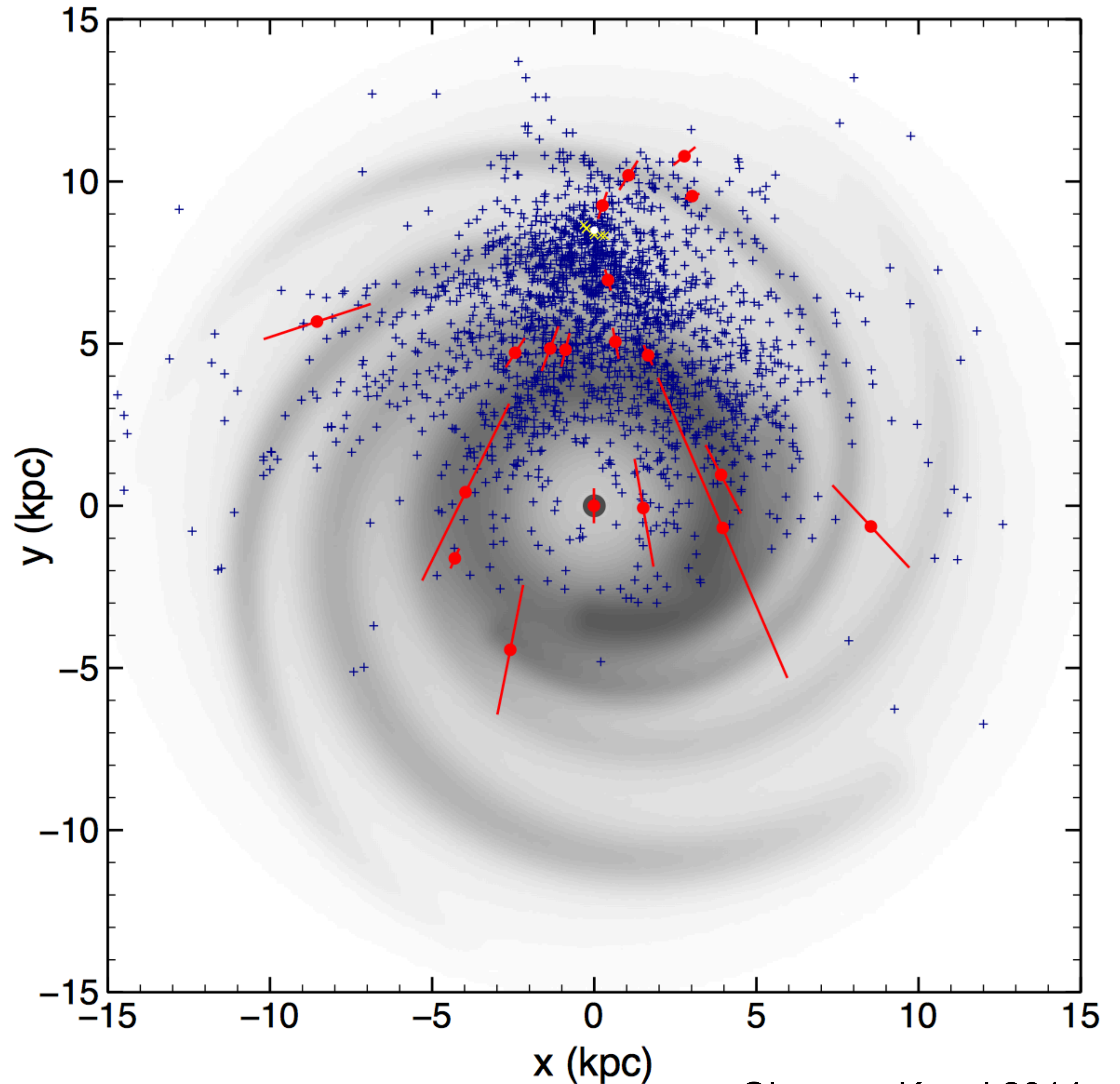
Neutron stars hold long-lived ultrastrong magnetic fields; become alive and bursting when $B \gg 10^{14}$ G (“magnetars”)

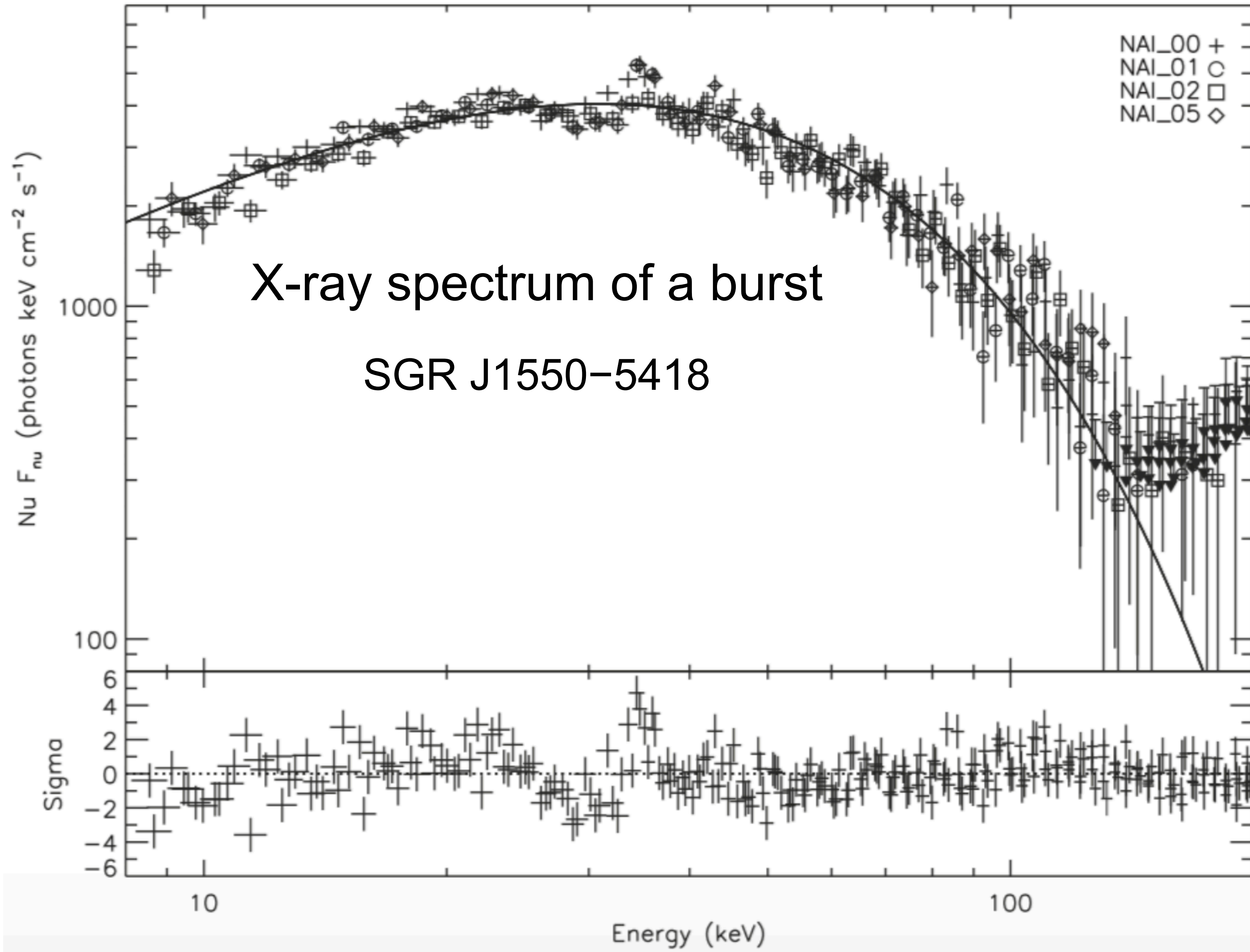
Magnetars

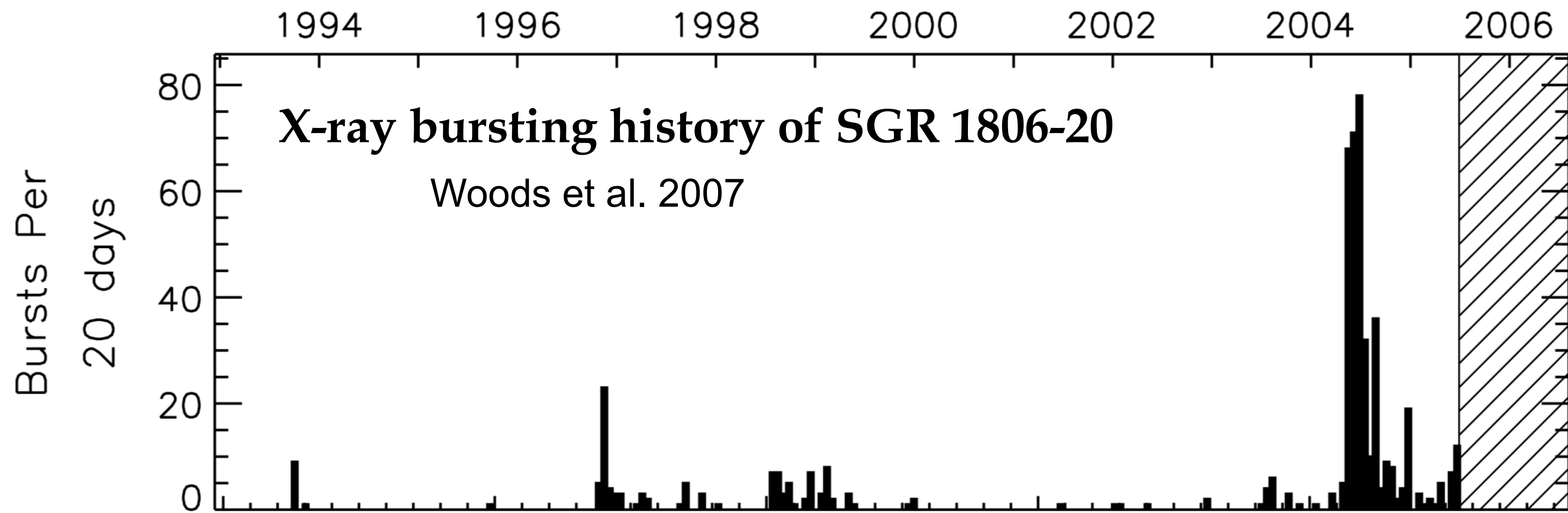
– bursting neutron stars
powered by
magnetic energy

- >10% of NS are born as magnetars
- active ~10 kyr
- spin $P = 2-12$ s

Why bursting?







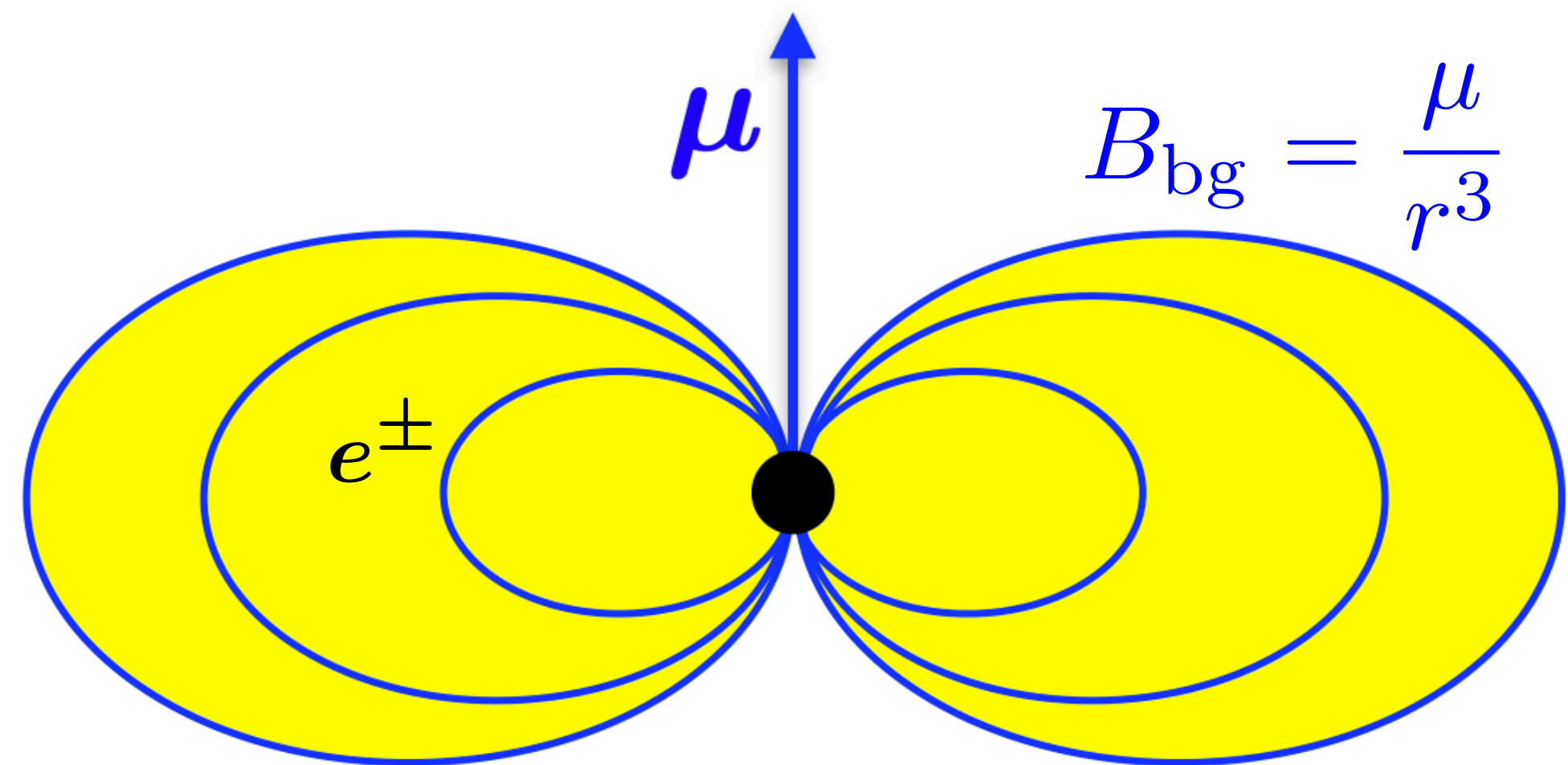
events of fast dissipation of magnetic energy

Burst durations ~ 0.1 s luminosities $10^{41} - 10^{47}$ erg/s

Thompson, Duncan 1995: starquakes excite magnetospheric Alfvén waves

New: quakes produce monster shocks and ejecta, emitting X-ray and radio bursts

Magnetosphere of a neutron star



– perturbed by quakes

perturbation frequency in kHz band

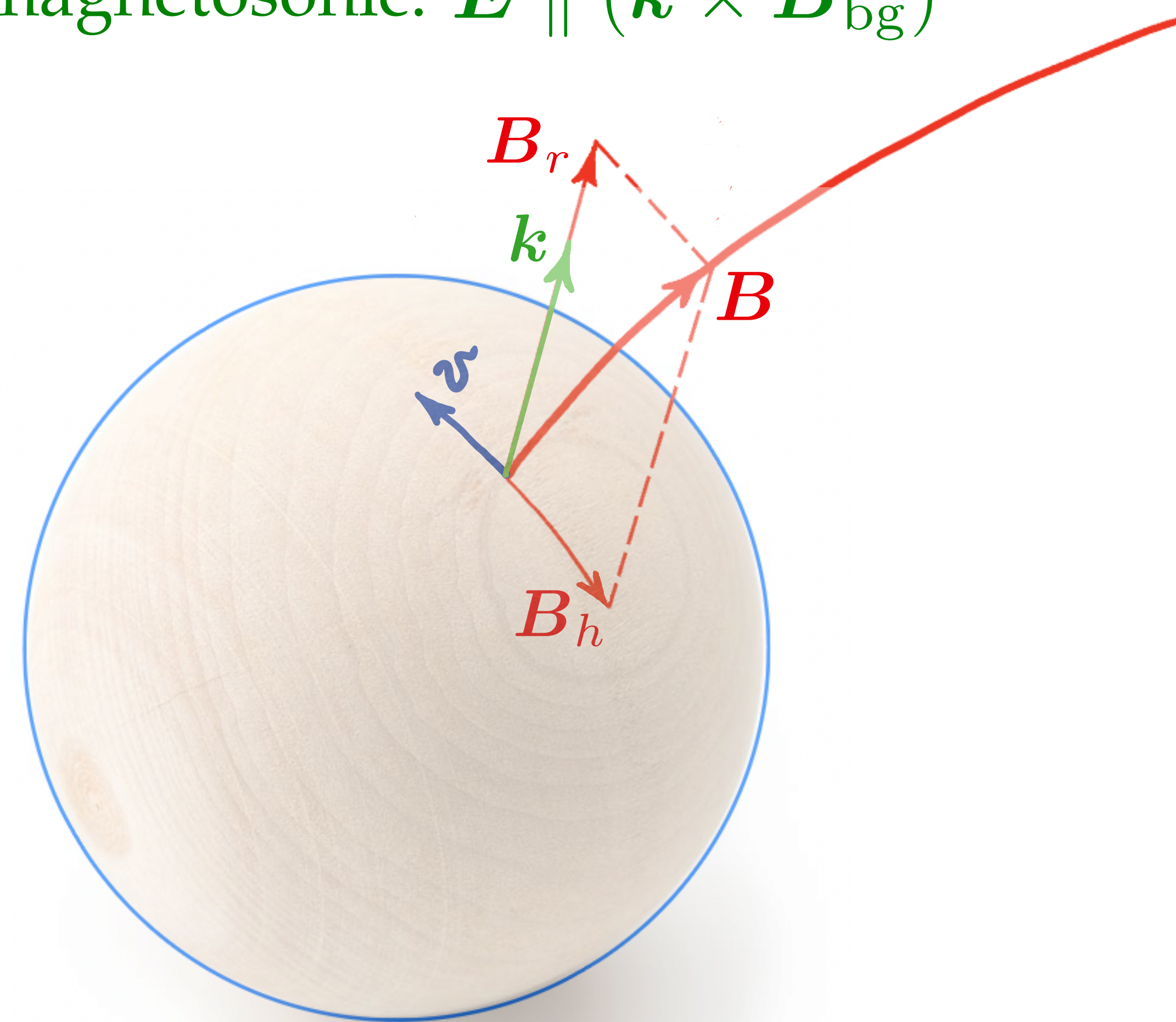
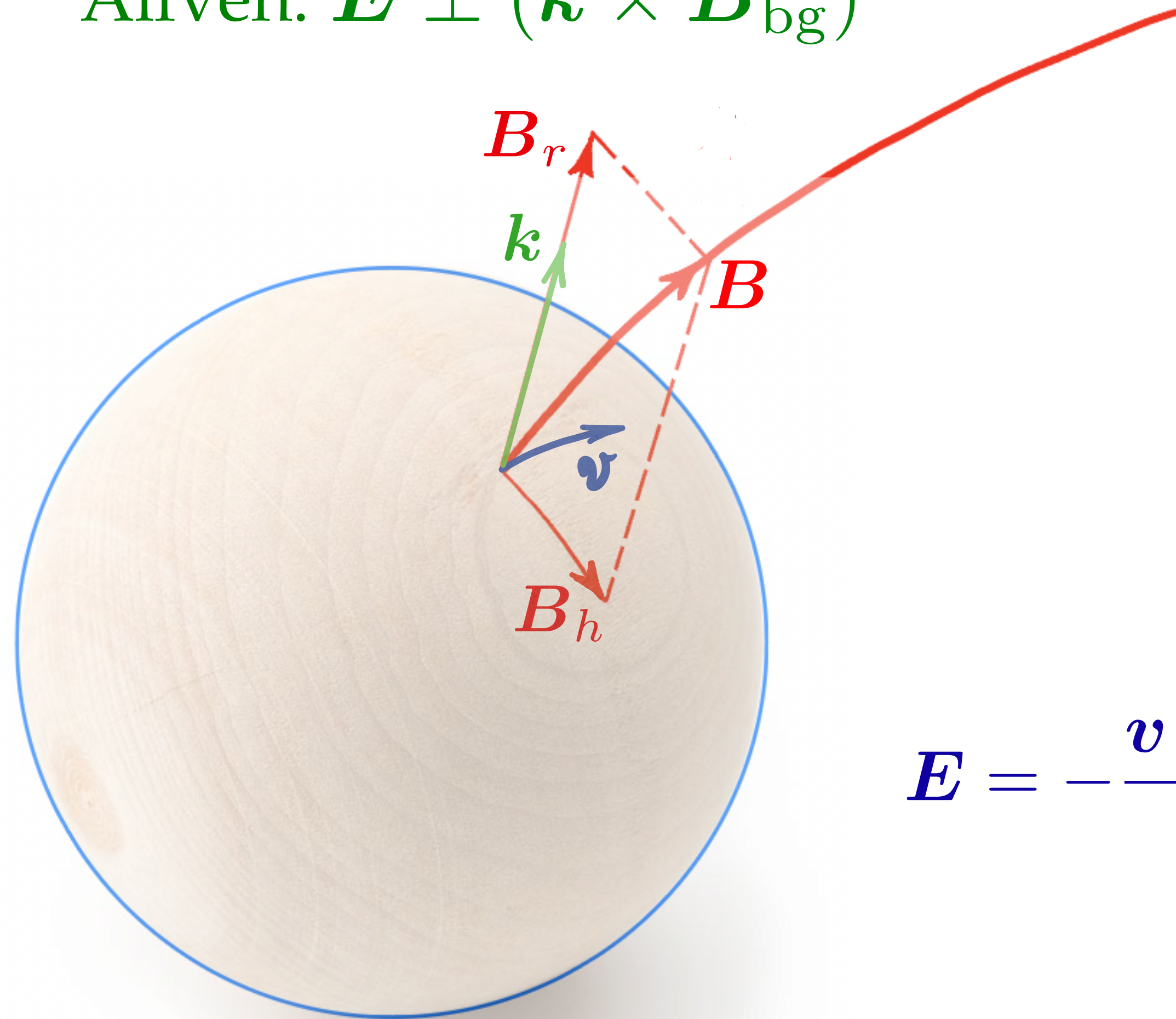
$$L \approx 10^{46} \left(\frac{\delta B_{\star}}{10^{12} \text{ G}} \right)^2 \frac{\text{erg}}{\text{s}}$$

$\delta B_{\star} \ll B_{\star}$ at the star; $\delta B / B_{\text{bg}}$ grows as the wave propagates outward

Wave emission by quakes (kHz)

Alfven: $\mathbf{E} \perp (\mathbf{k} \times \mathbf{B}_{bg})$

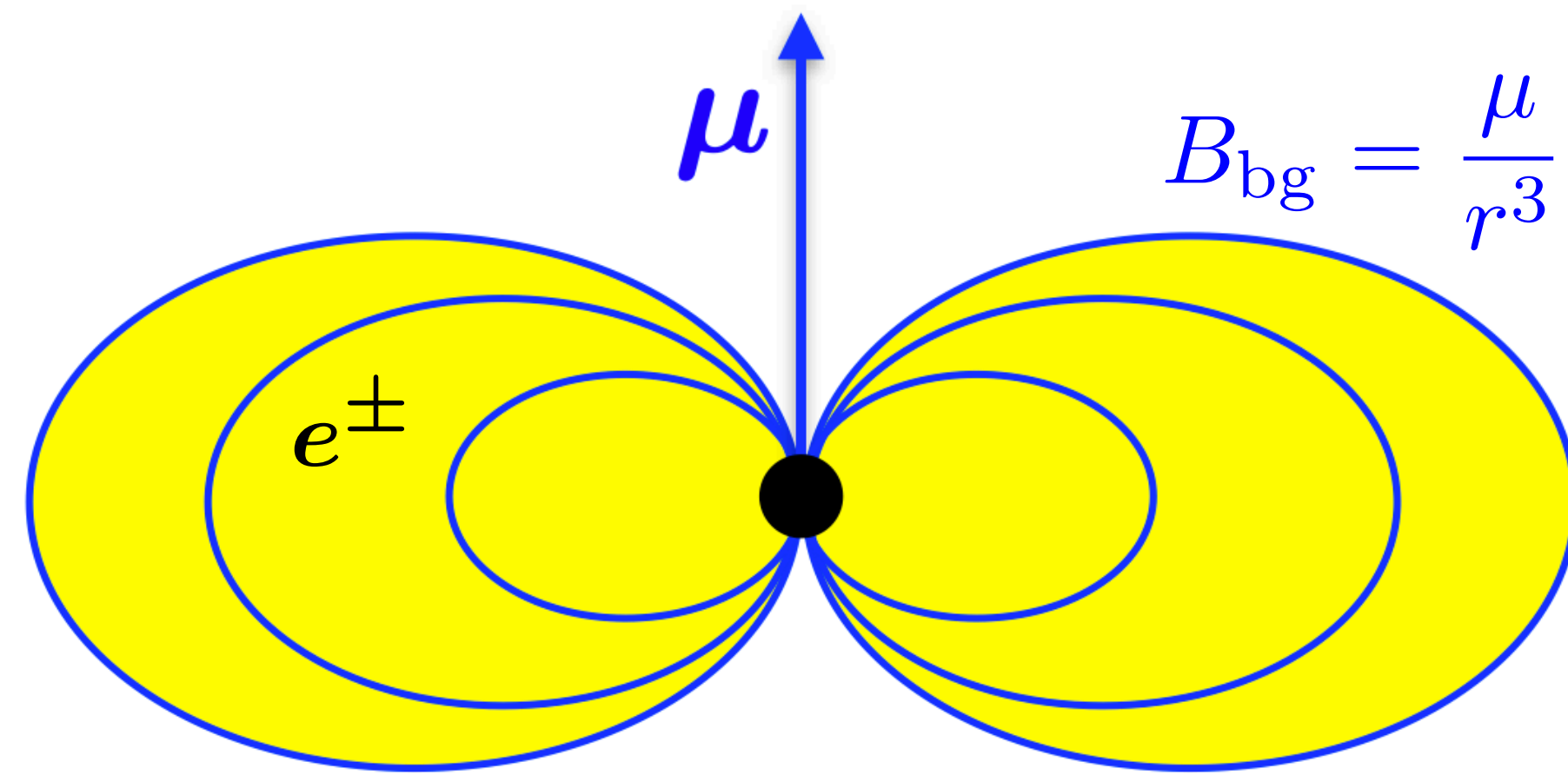
magnetosonic: $\mathbf{E} \parallel (\mathbf{k} \times \mathbf{B}_{bg})$



$$\mathbf{E} = -\frac{\mathbf{v} \times \mathbf{B}}{c}$$

(+ waves from instabilities in the magnetosphere itself, see Jens Mahlmann's talk)

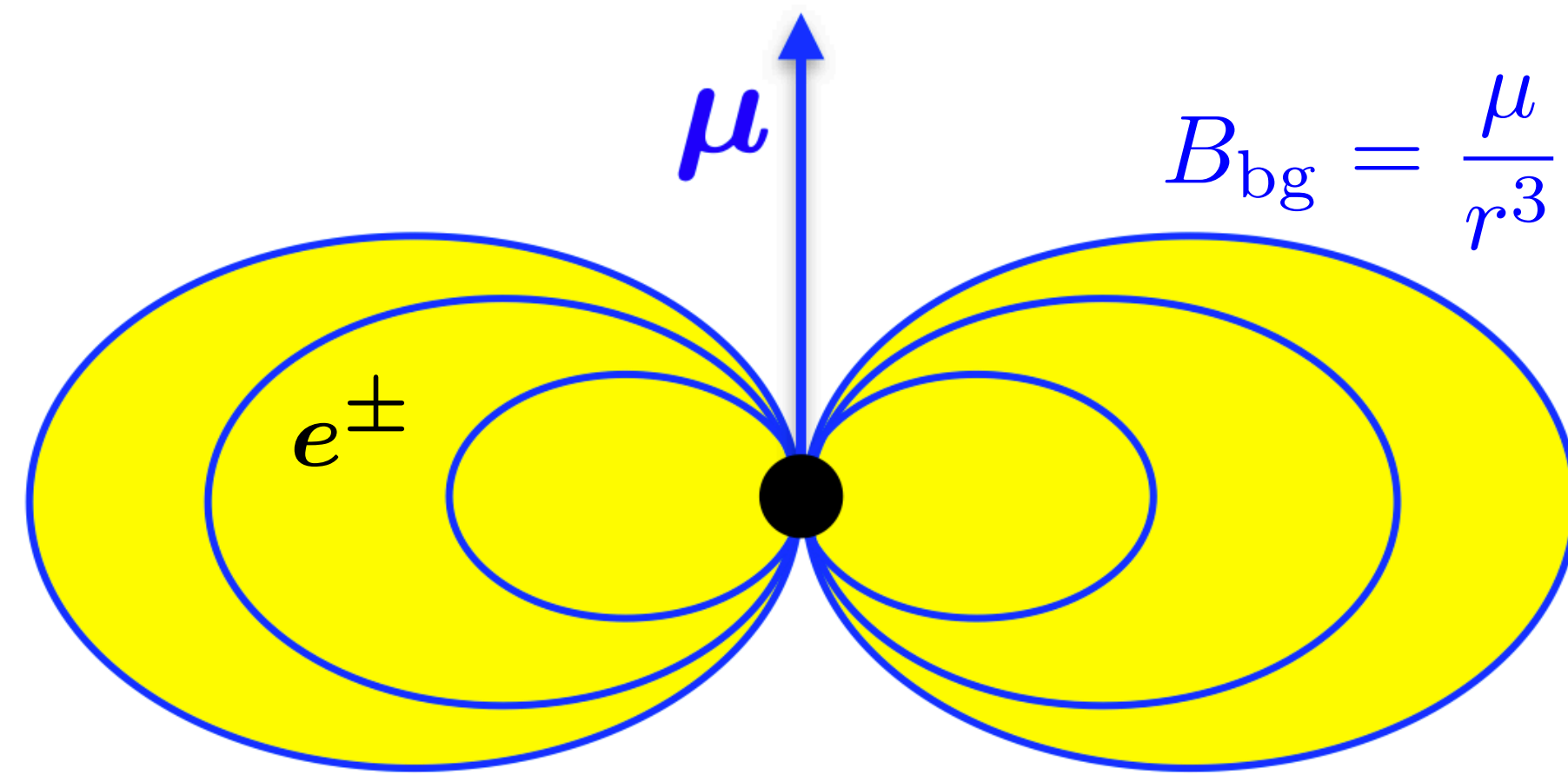
I. Magnetosonic waves



$$\sigma_{\text{bg}} = \frac{B_{\text{bg}}^2}{4\pi n_{\text{bg}} m_e c^2} \sim 10^{10} r_8^{-3}$$

Magnetosonic modes (compressive waves): $\frac{v_{\text{wave}}}{c} = 1 - \sigma_{\text{bg}}^{-1}$

$\sigma_{\text{bg}} \rightarrow \infty$: fast magnetosonic mode \rightarrow vacuum electromagnetic wave
(superimposed on B_{bg})

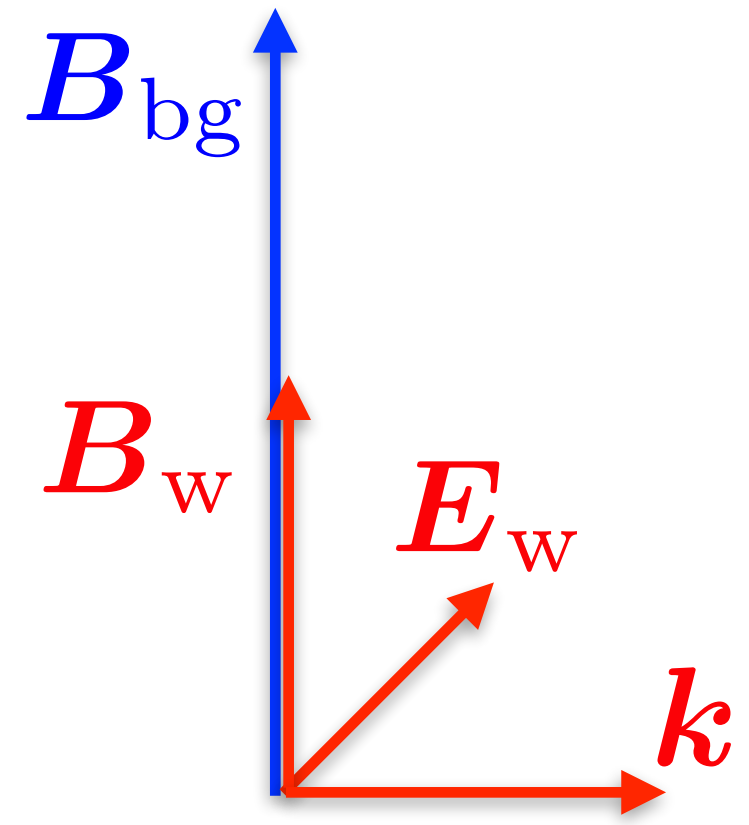


$$\sigma_{\text{bg}} = \frac{B_{\text{bg}}^2}{4\pi n_{\text{bg}} m_e c^2} \sim 10^{10} r_8^{-3}$$

Magnetosonic modes (compressive waves): $\frac{v_{\text{wave}}}{c} = 1 - \sigma_{\text{bg}}^{-1}$

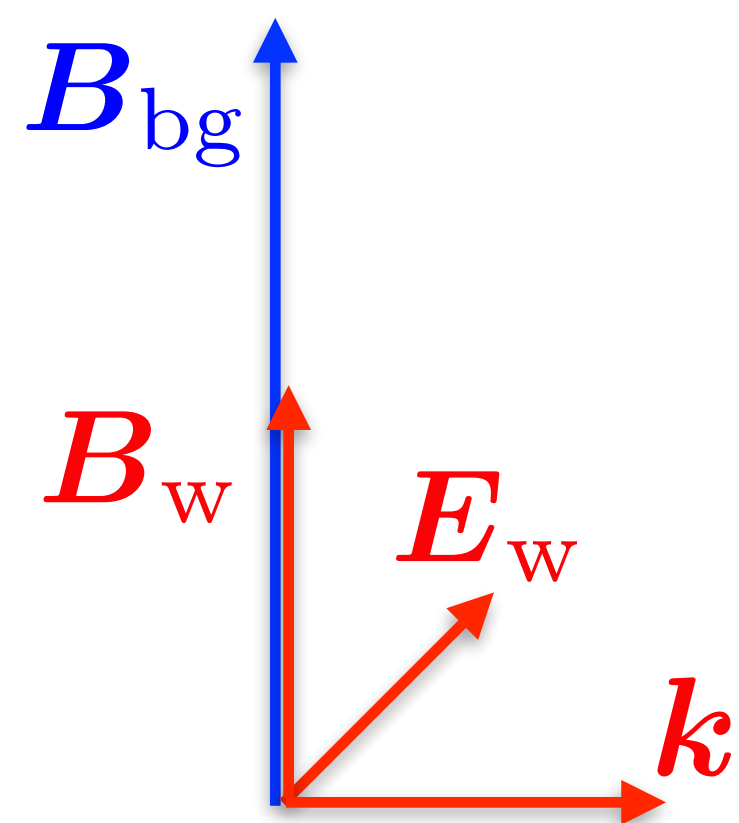
$\sigma_{\text{bg}} \rightarrow \infty$: fast magnetosonic mode \rightarrow vacuum electromagnetic wave
(superimposed on B_{bg})

$$\left. \begin{array}{l} \text{wave amplitude } E_0 \propto r^{-1} \\ \text{background field } B_{\text{bg}} \propto r^{-3} \end{array} \right\} \Rightarrow \frac{E_0}{B_{\text{bg}}} \propto r^2$$



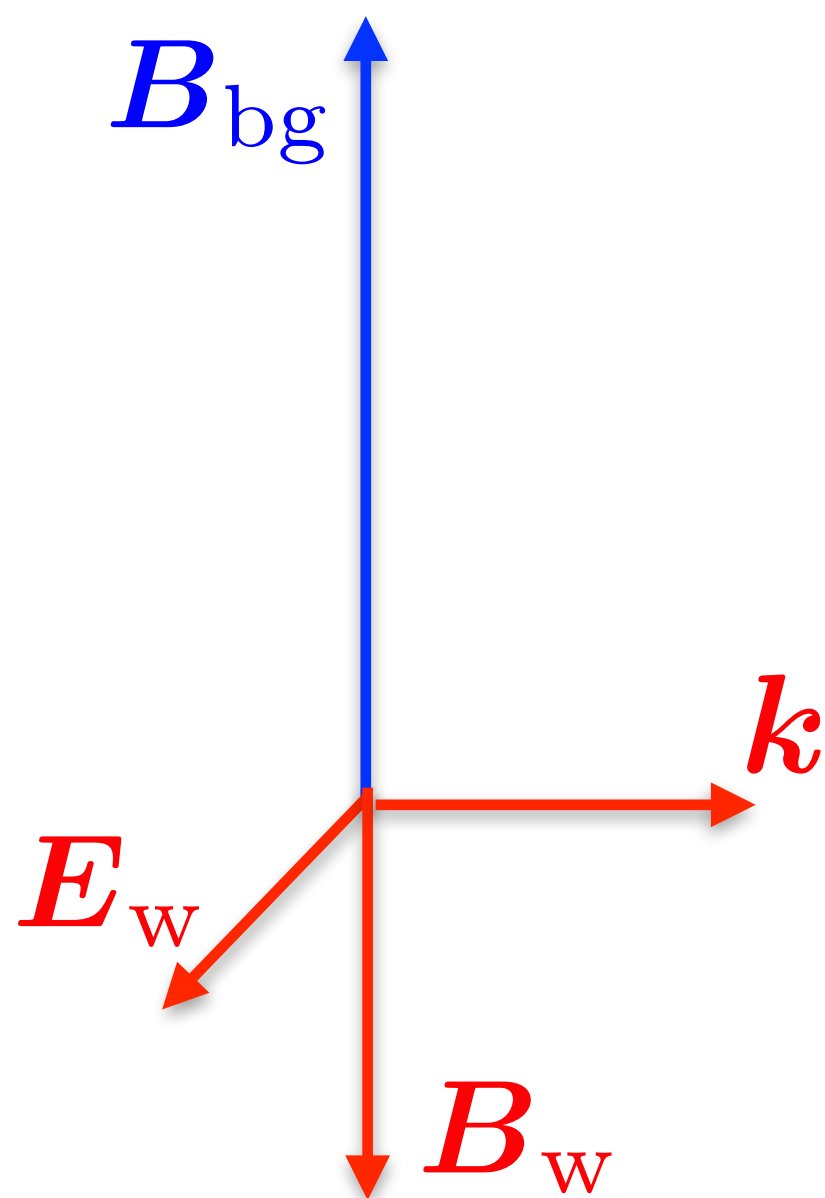
$$\mathbf{B} = \mathbf{B}_{bg} + \mathbf{B}_w$$

$$\mathbf{E} = \mathbf{E}_w$$



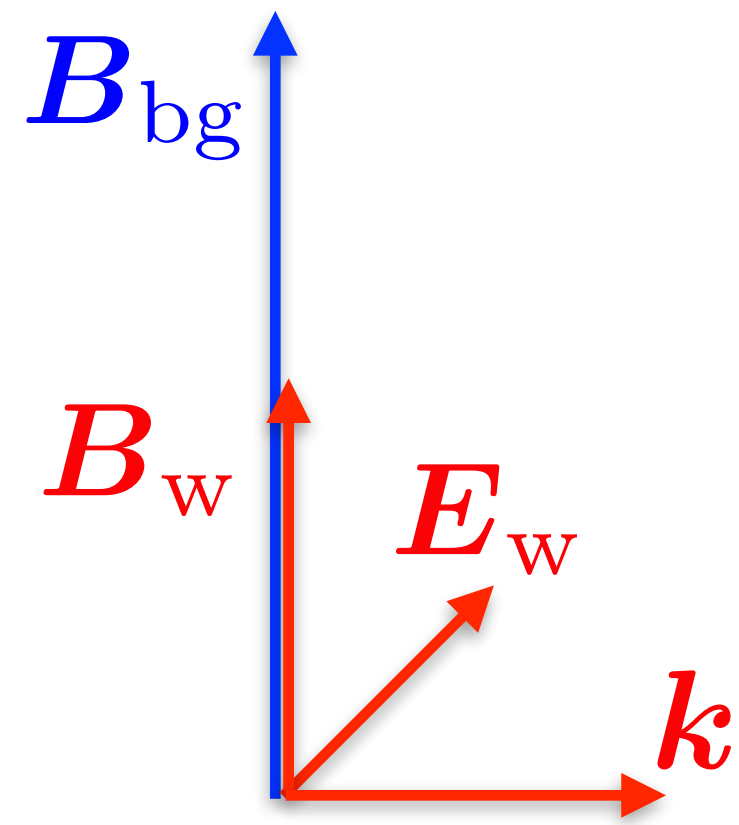
$$\mathbf{B} = \mathbf{B}_{\text{bg}} + \mathbf{B}_{\text{w}}$$

$$\mathbf{E} = \mathbf{E}_{\text{w}}$$



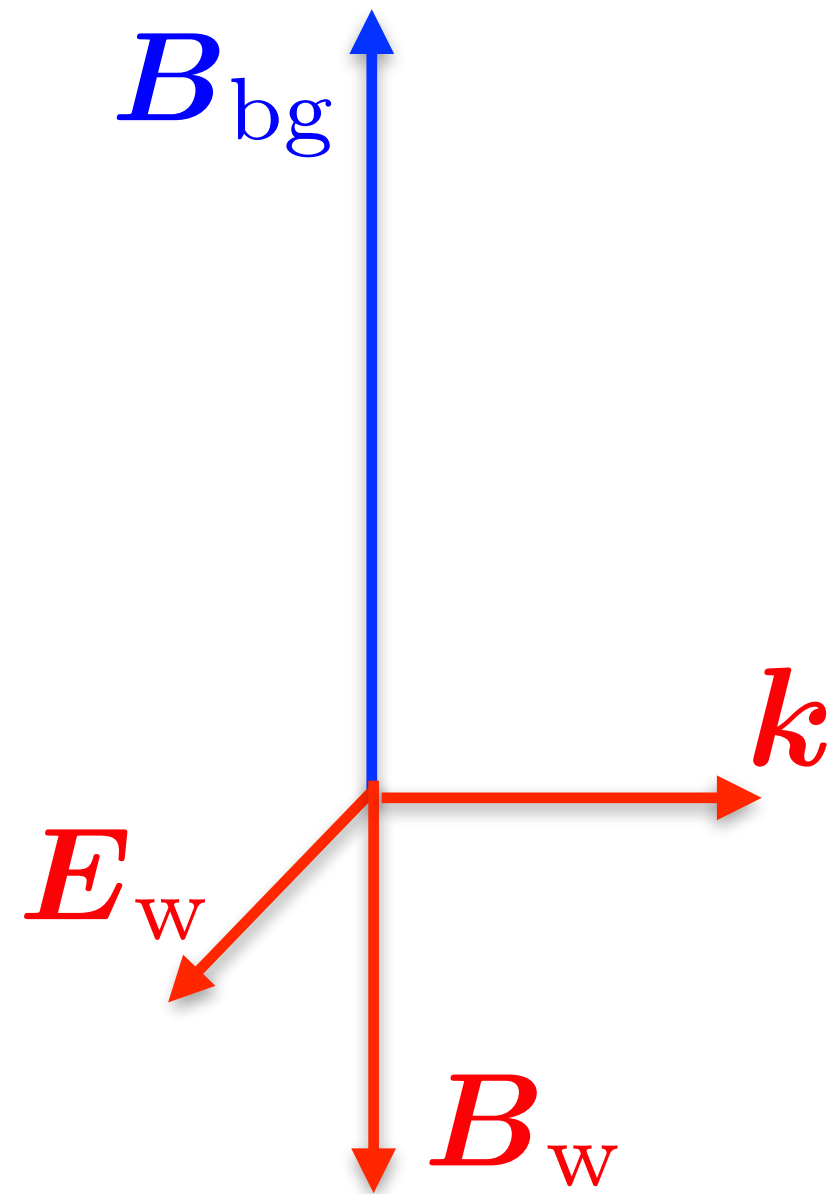
plasma motion in the wave: $\frac{\mathbf{v}_D}{c} = \frac{\mathbf{E} \times \mathbf{B}}{B^2}$

$$\frac{|\mathbf{v}_D|}{c} = \frac{|\mathbf{E}|}{|\mathbf{B}|}$$



$$\mathbf{B} = \mathbf{B}_{\text{bg}} + \mathbf{B}_{\text{w}}$$

$$\mathbf{E} = \mathbf{E}_{\text{w}}$$



wave breaks when

$$|\mathbf{E}| = |\mathbf{B}| = \frac{B_{\text{bg}}}{2}$$

$$(v_{\text{D}} \rightarrow -c)$$

occurs at $R_{\times} \sim 10^8$ cm

plasma motion in the wave: $\frac{v_{\text{D}}}{c} = \frac{\mathbf{E} \times \mathbf{B}}{B^2}$

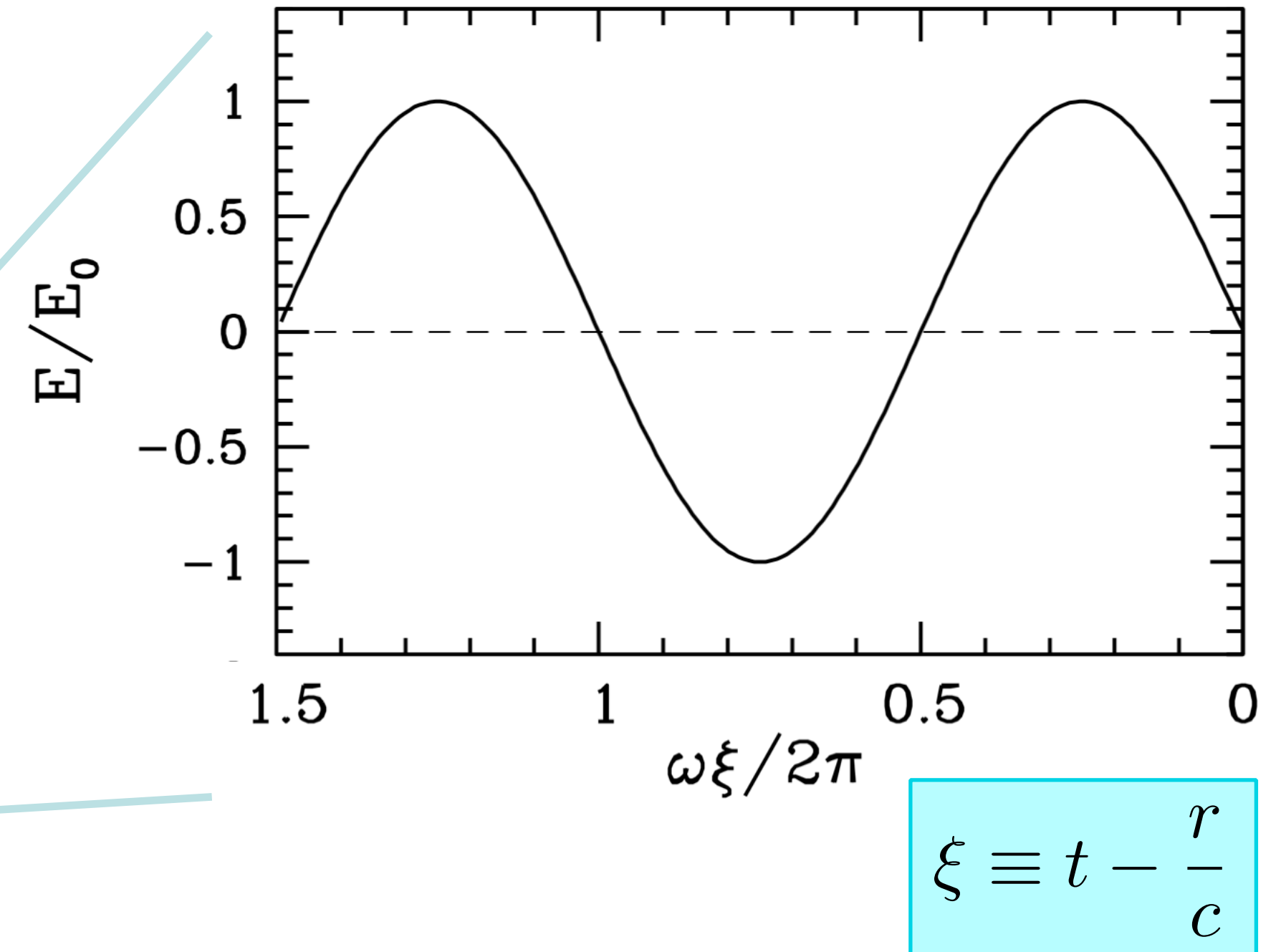
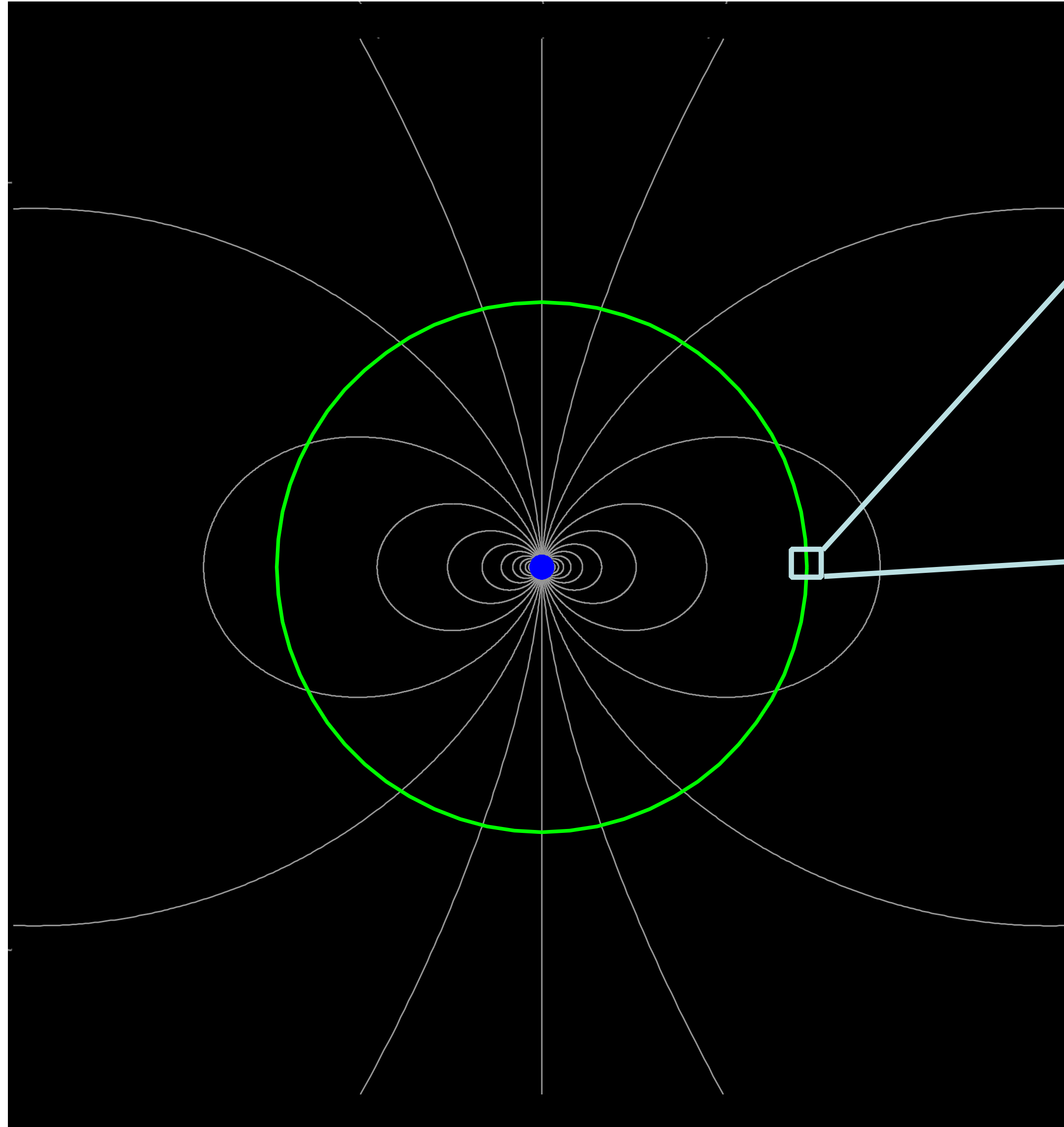
$$\frac{|v_{\text{D}}|}{c} = \frac{|\mathbf{E}|}{|\mathbf{B}|}$$

shock formation:

PIC simulation:
Chen et al. 2022

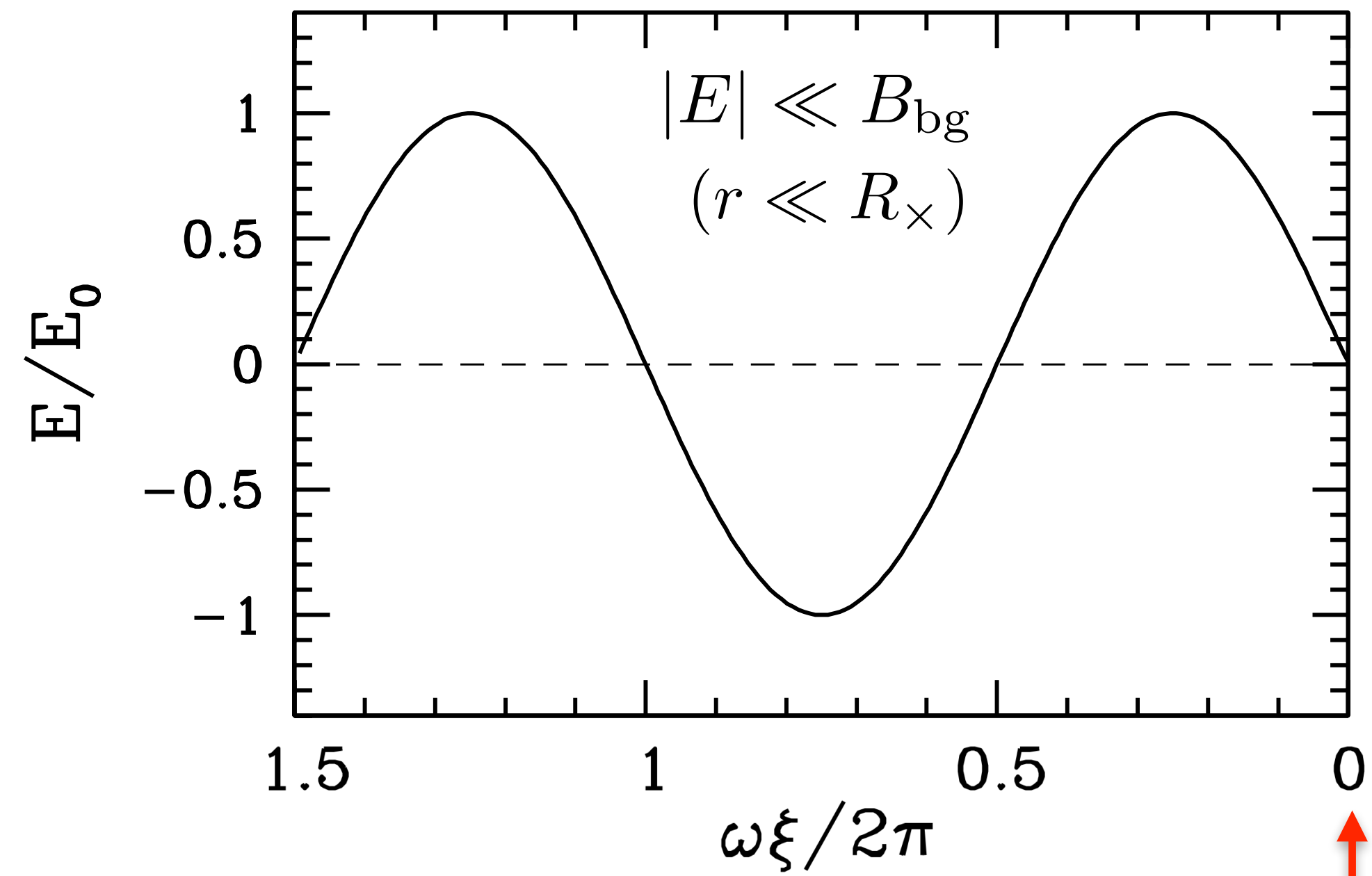
MHD:
AB 2022

an expanding EM wave packet



- find the MHD solution for the wave expansion through the dipole magnetosphere

(AB, ApJ in press)

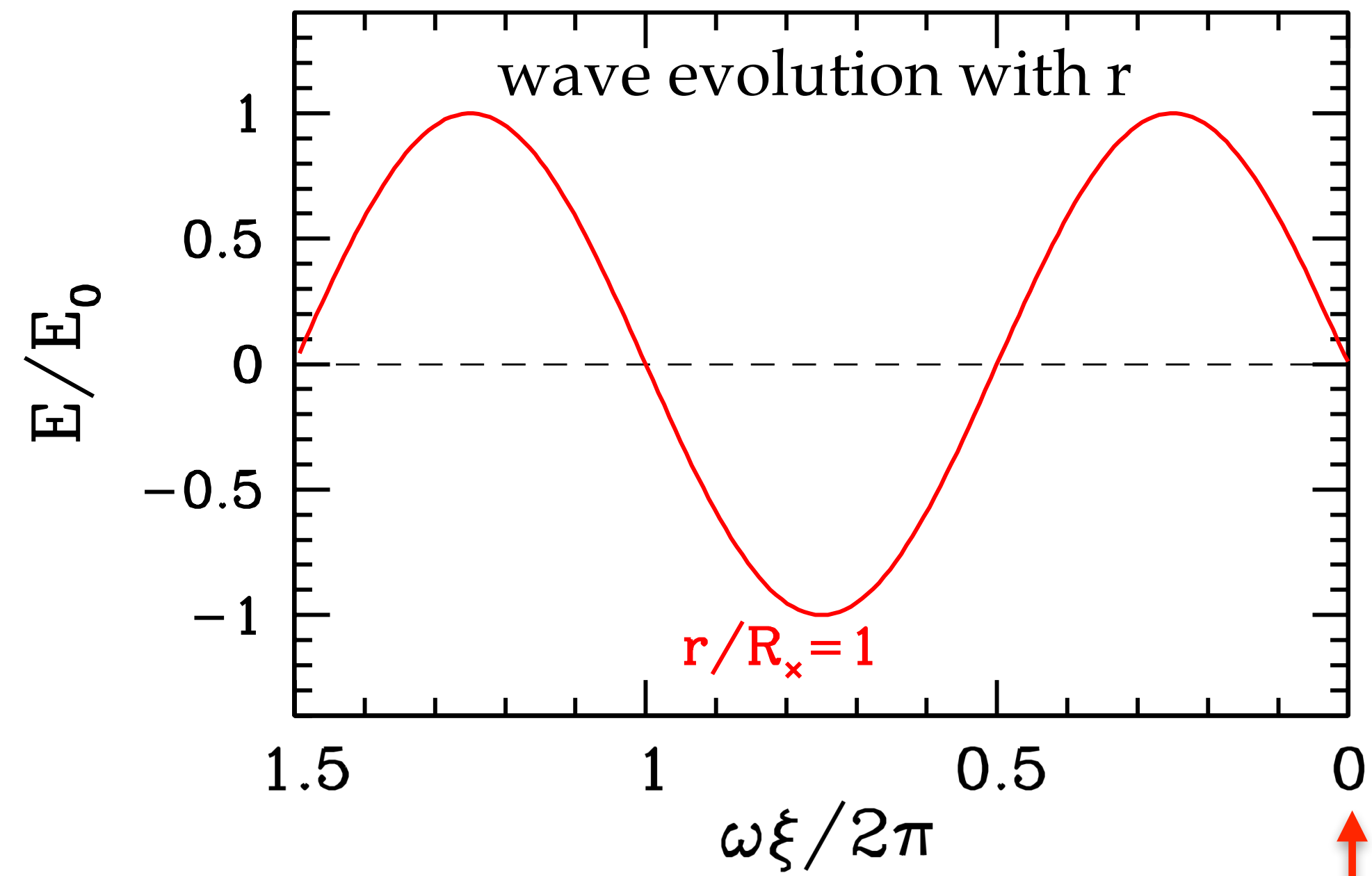


initial profile:

$$E(\xi) = E_0 \sin(\omega\xi)$$

$$\xi \equiv t - \frac{r}{c}$$

↑
beginning of
the kHz wave

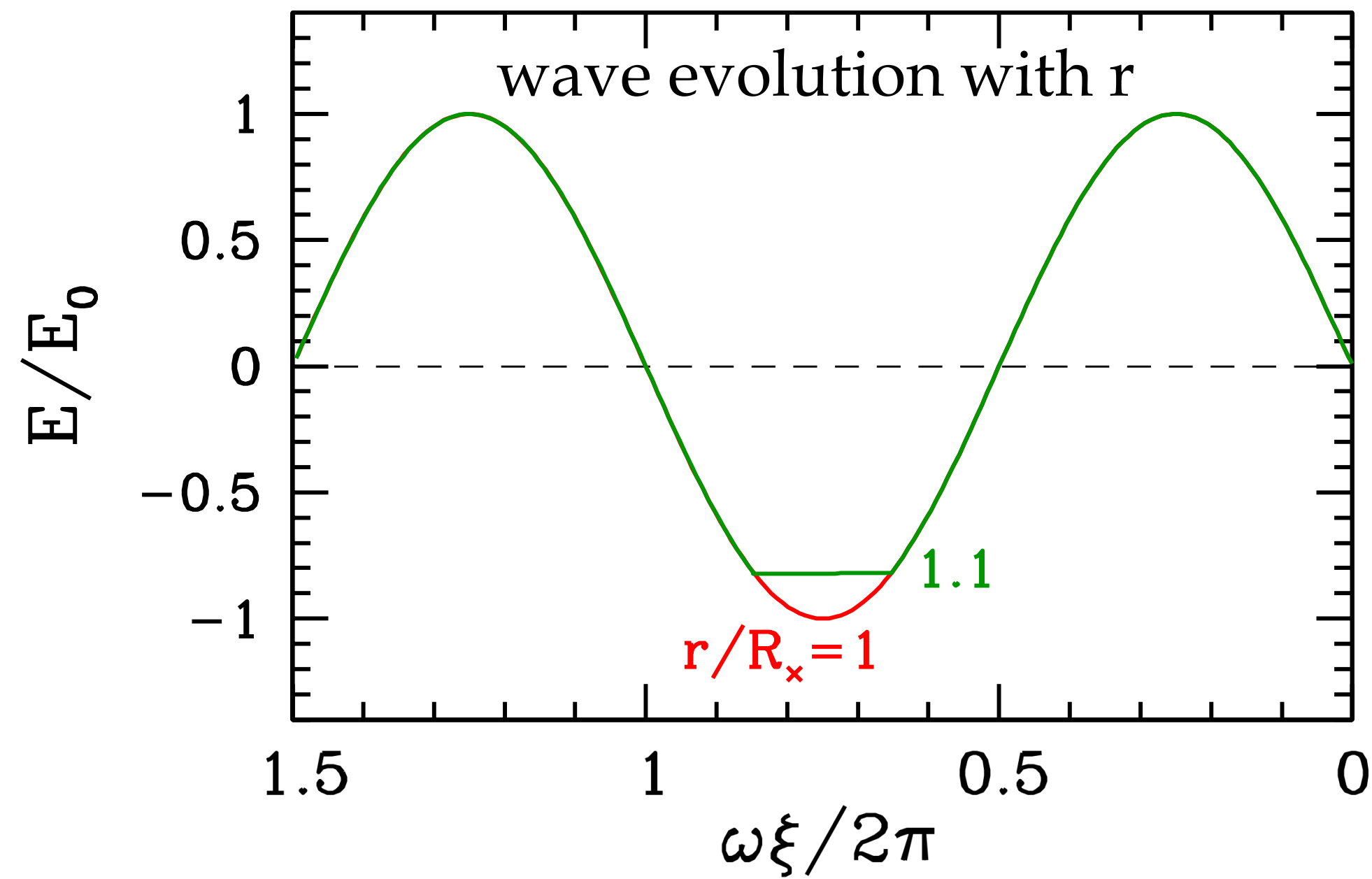


initial profile:

$$E(\xi) = E_0 \sin(\omega\xi)$$

$$\xi \equiv t - \frac{r}{c}$$

beginning of
the kHz wave



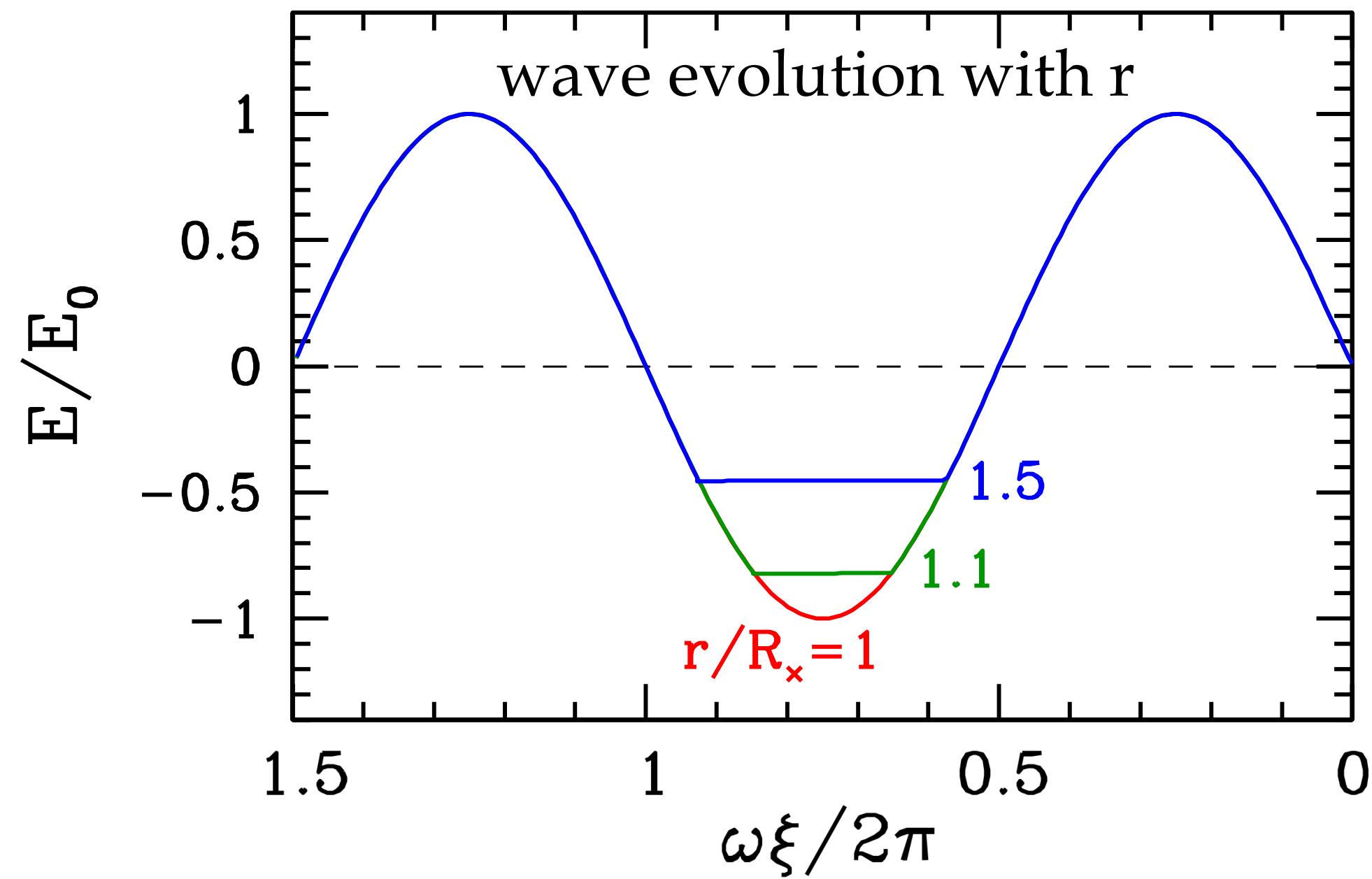
initial profile:

$$E(\xi) = E_0 \sin(\omega\xi)$$

$$\xi \equiv t - \frac{r}{c}$$

Plateau: the ceiling of $E^2 = B^2$ corresponds to $|E_p| \approx \frac{B_{\text{bg}}}{2} \propto r^{-3}$

instead of the vacuum solution $E \propto r^{-1}$



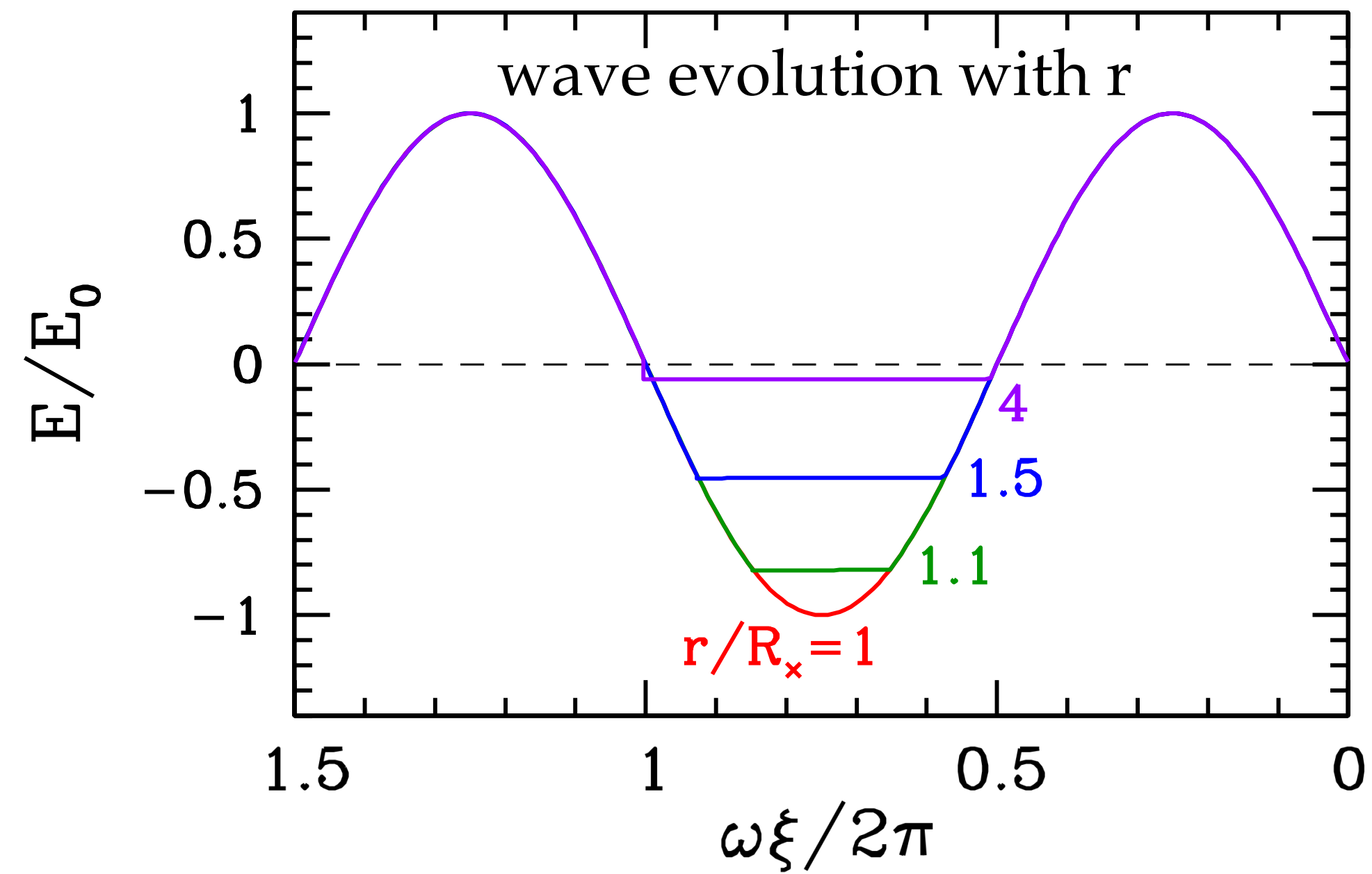
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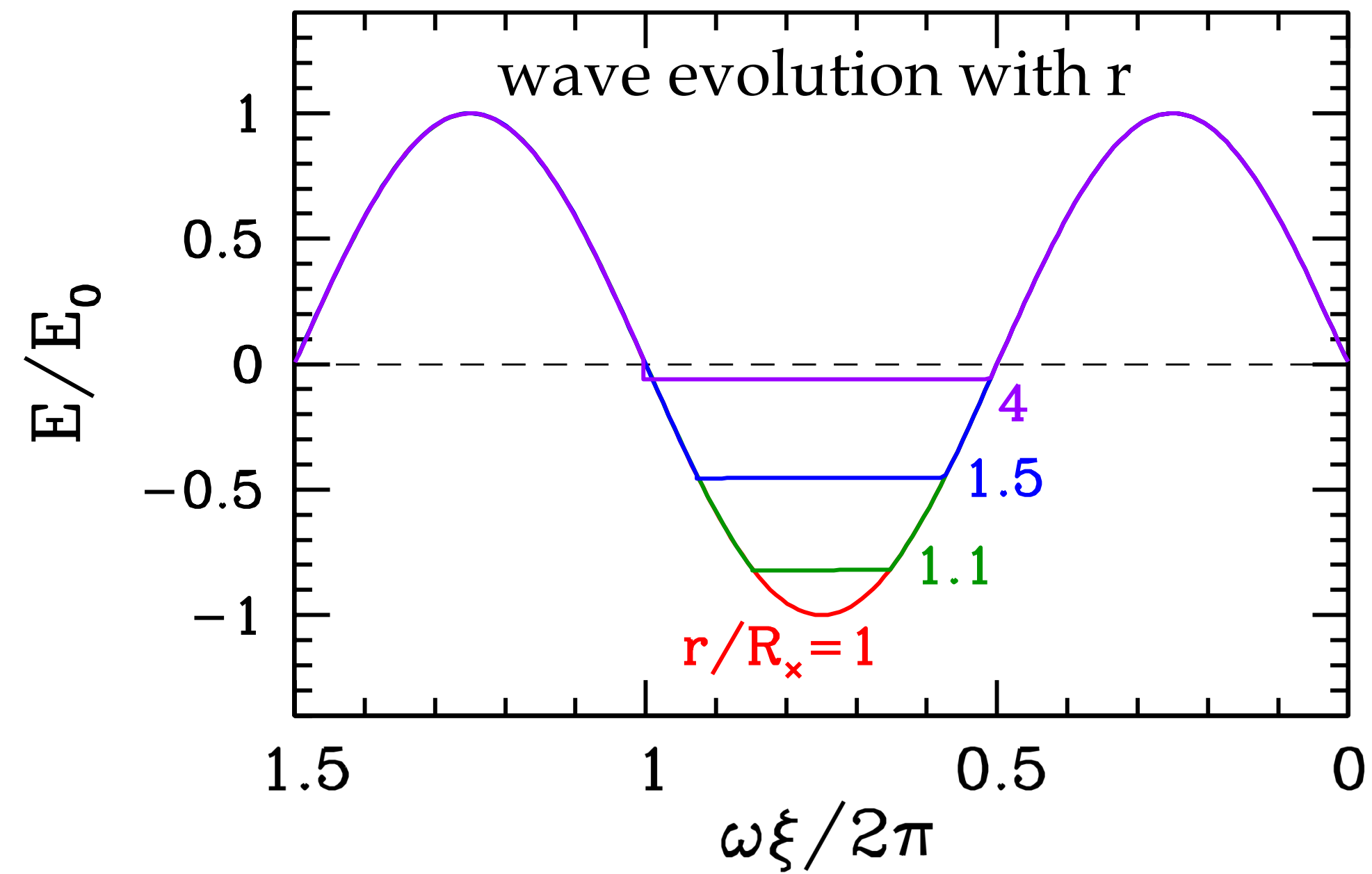
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initial profile: $E(\xi) = E_0 \sin(\omega\xi)$

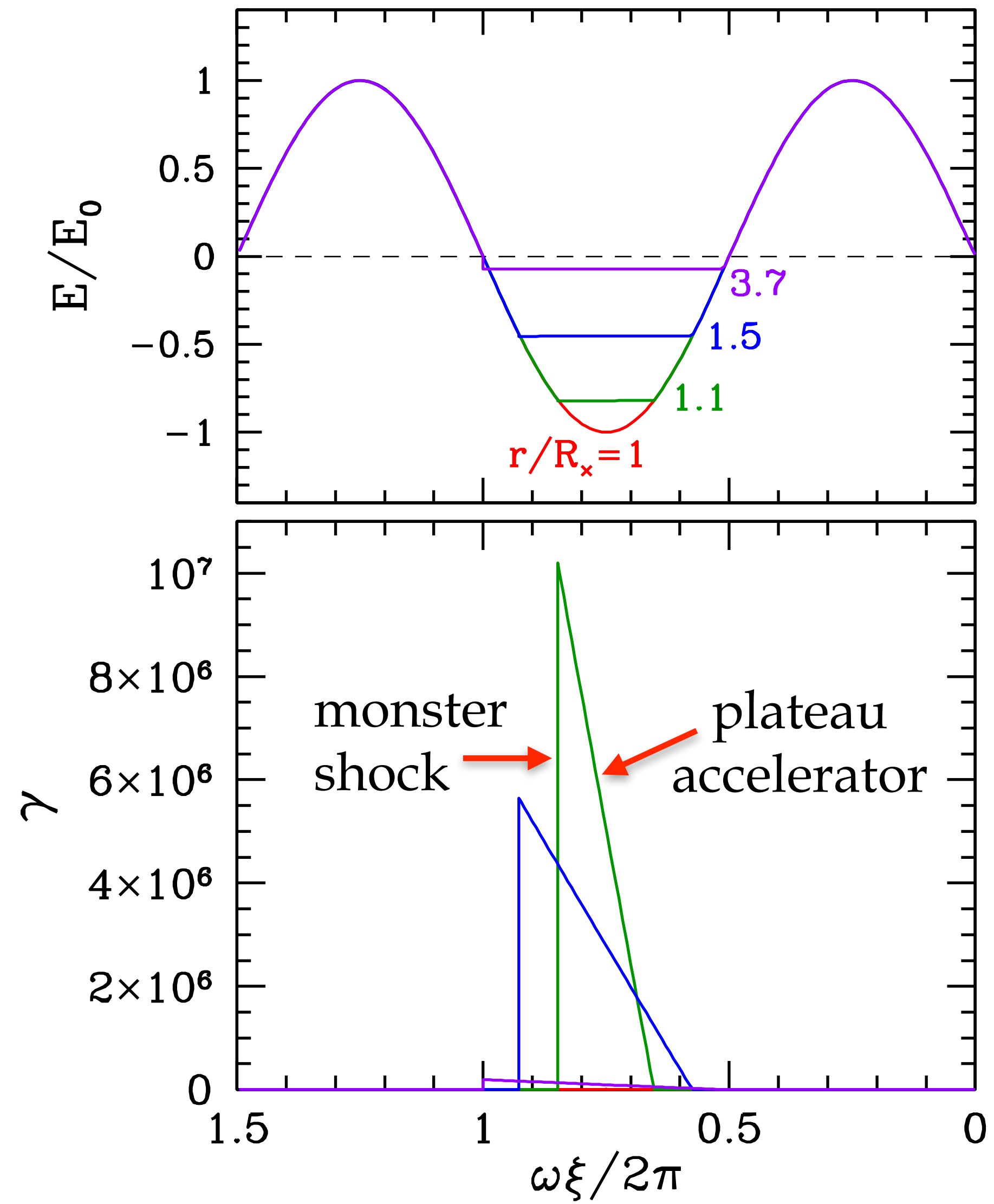
$$\xi \equiv t - \frac{r}{c}$$

Plateau: the ceiling of $E^2 = B^2$ corresponds to $|E_p| \approx \frac{B_{\text{bg}}}{2} \propto r^{-3}$

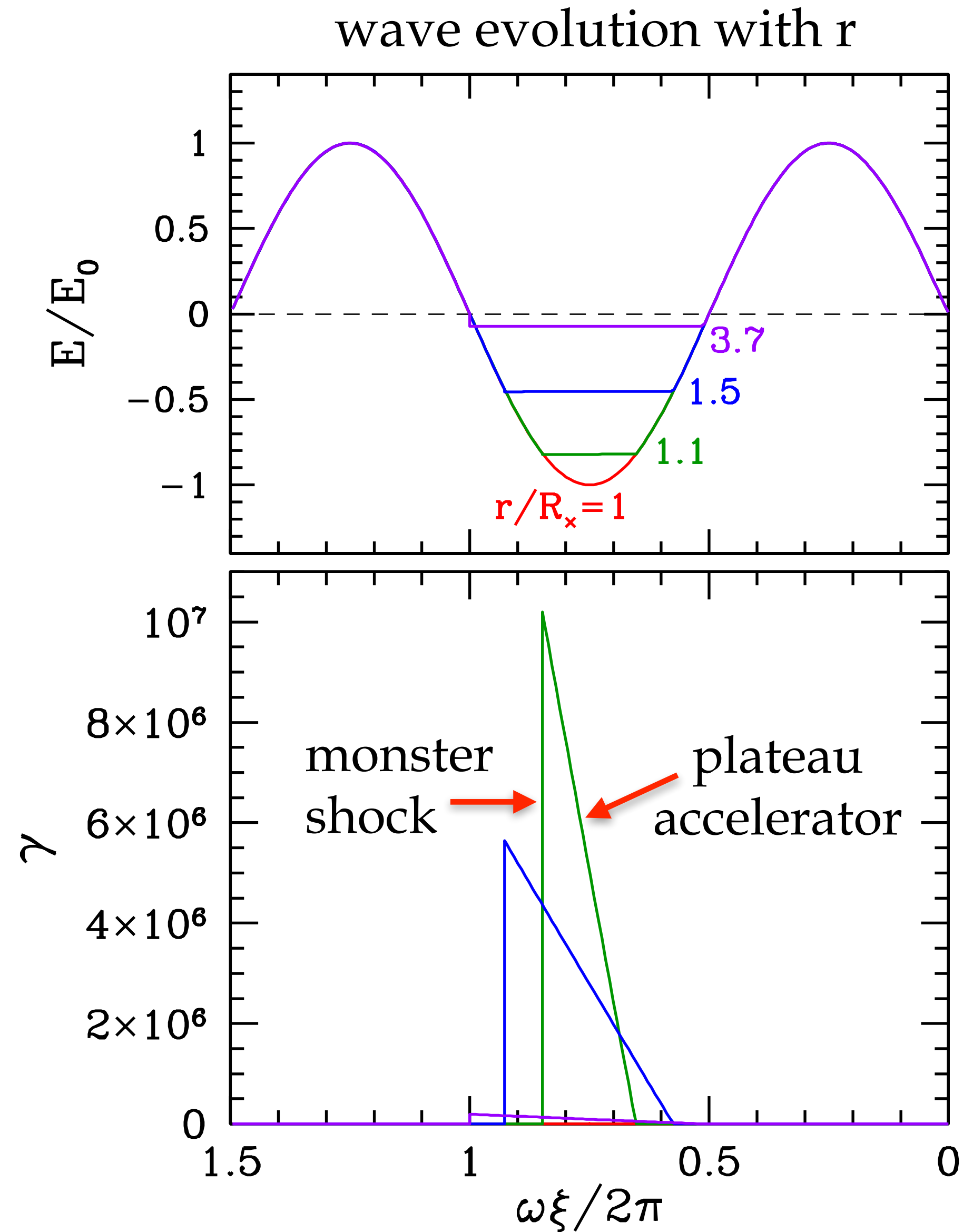
instead of the vacuum solution $E \propto r^{-1}$

where did the half-wave energy go?

wave evolution with r



$$n m c^2 \frac{d\gamma}{dt} = \mathbf{E} \cdot \mathbf{j}$$



$$n m c^2 \frac{d\gamma}{dt} = \mathbf{E} \cdot \mathbf{j}$$

plateau: a linear accelerator

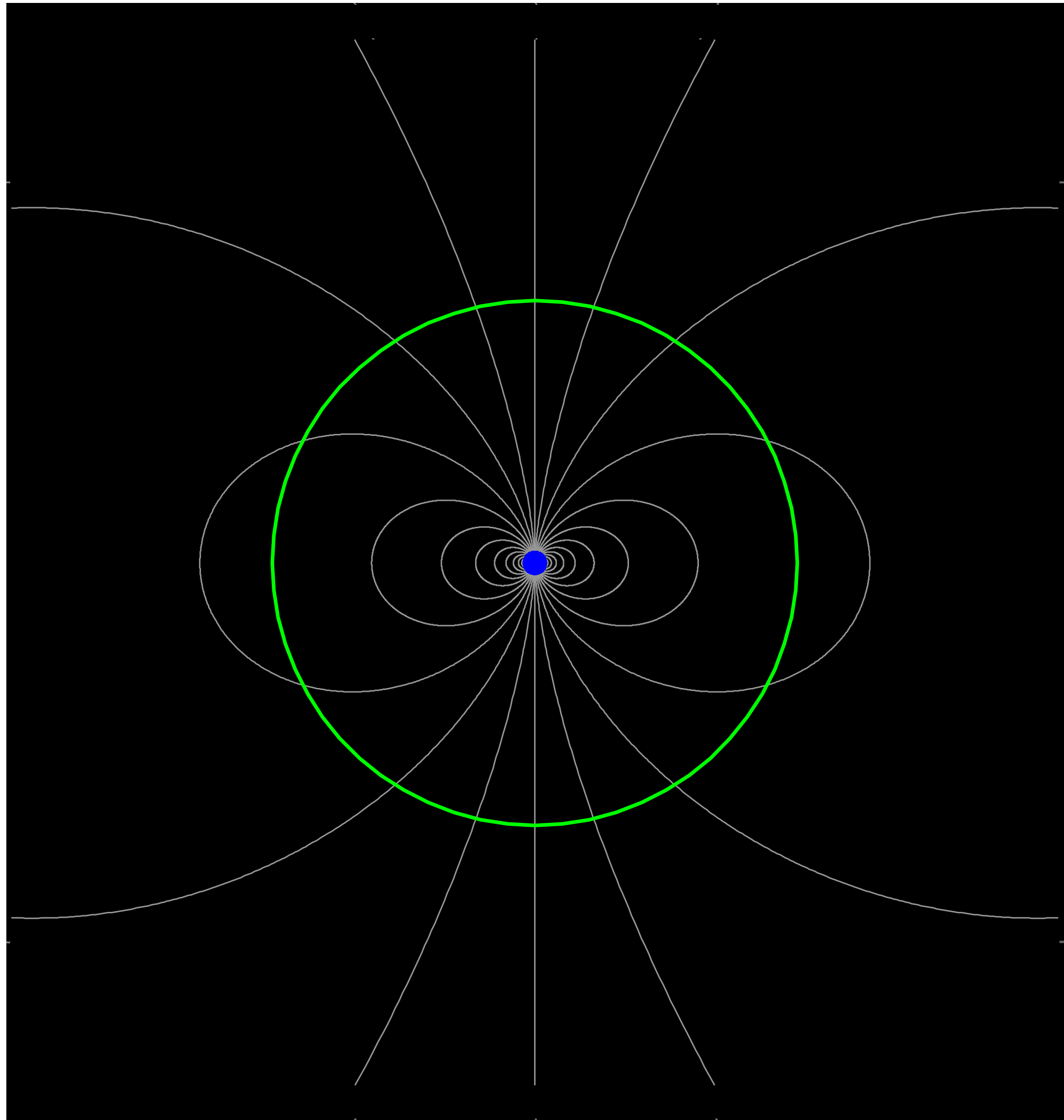
plateau width $W_p \sim \frac{c}{\omega}$

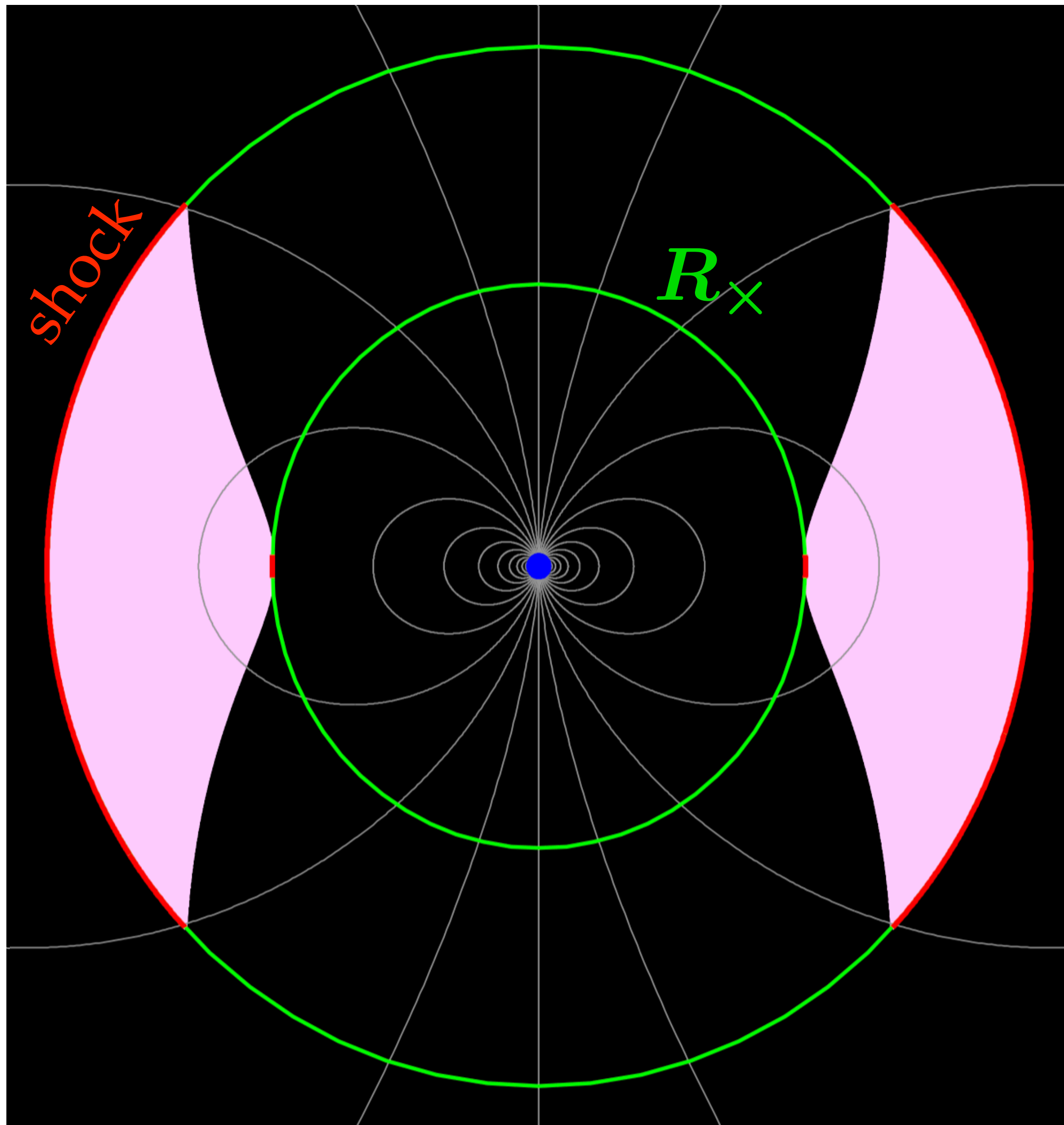
$$\gamma = \frac{W_p}{r} \sigma_{bg} \sim 10^7 !$$

shock at the end of the plateau

monster shock weakens as it expands inside the magnetosphere, and again becomes strong outside.

relativistic explosion in the magnetar wind





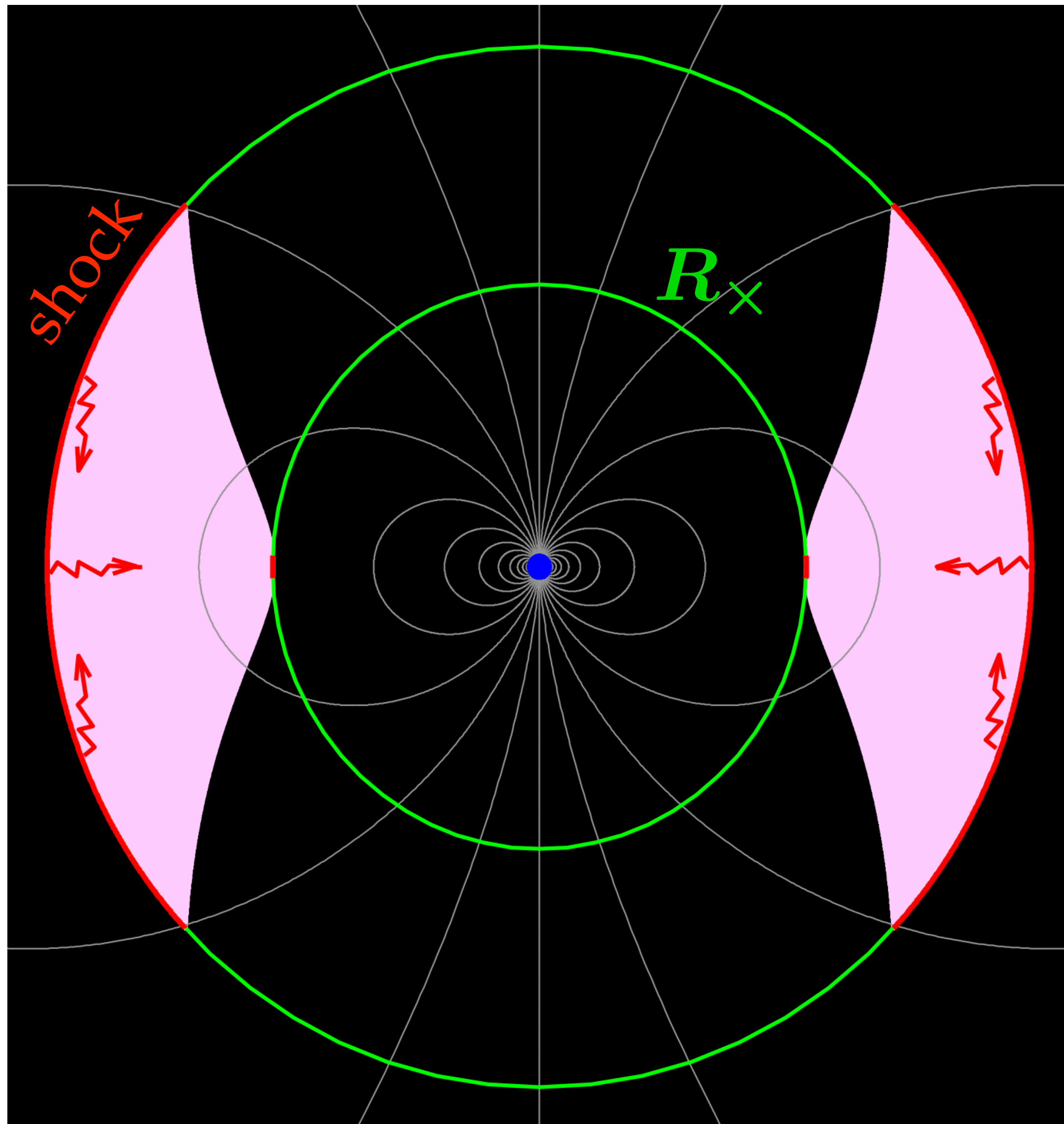
magnetic dipole moment
of the star

$$R_x = \left(\frac{c\mu^2}{8L} \right)^{1/4} \quad (E^2 = B^2)$$

wave power

Example: $L = 10^{43}$ erg/s

$$R_x \approx 100R_*$$



Monster shocks are radiative

particles crossing the shock
emit curvature gamma-rays

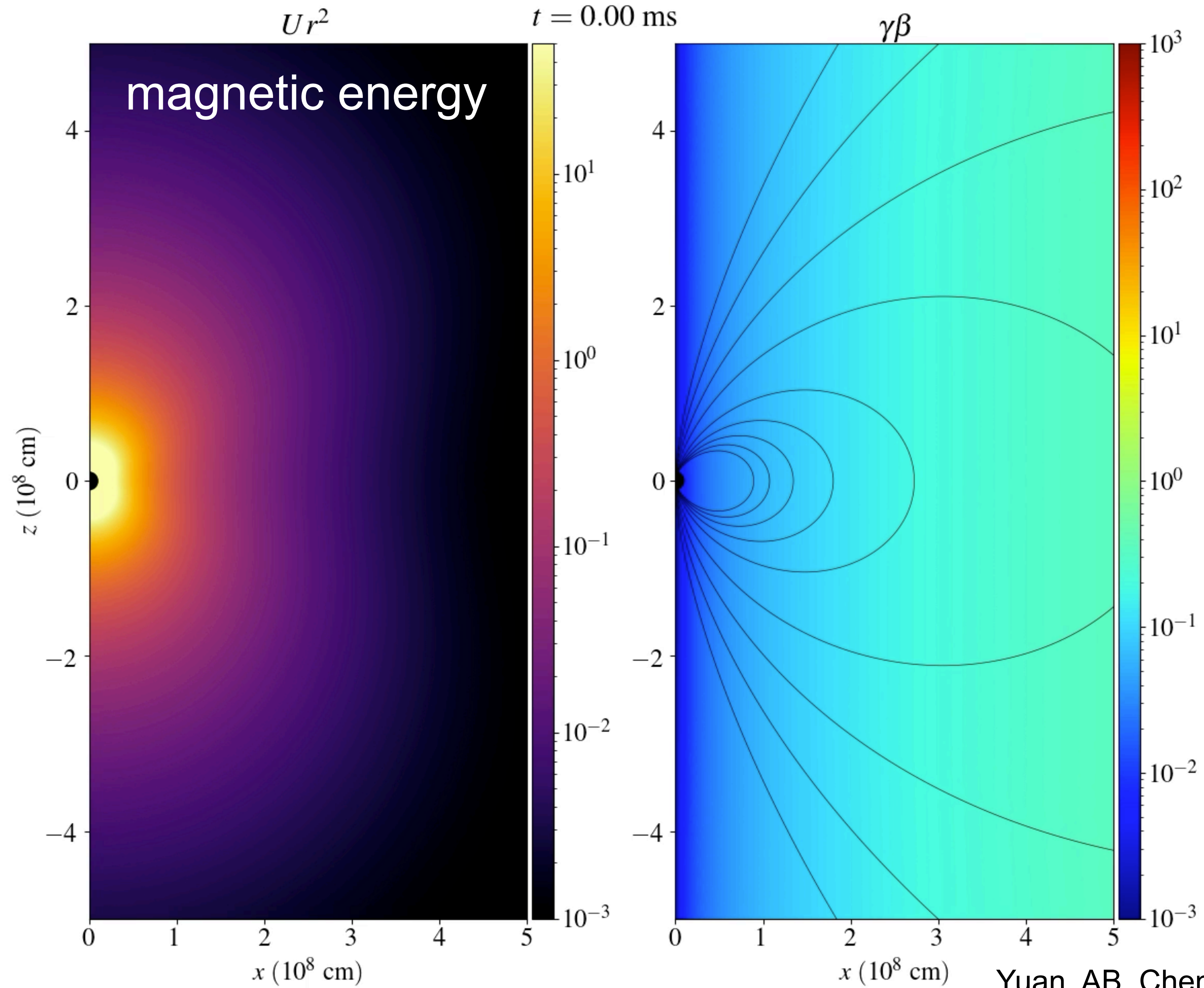
$$\text{Lorentz factor } \gamma \sim \frac{c \sigma_{\text{bg}}}{\omega R_x}$$

gamma-rays convert to e^+e^- pairs:
synchrotron cascade

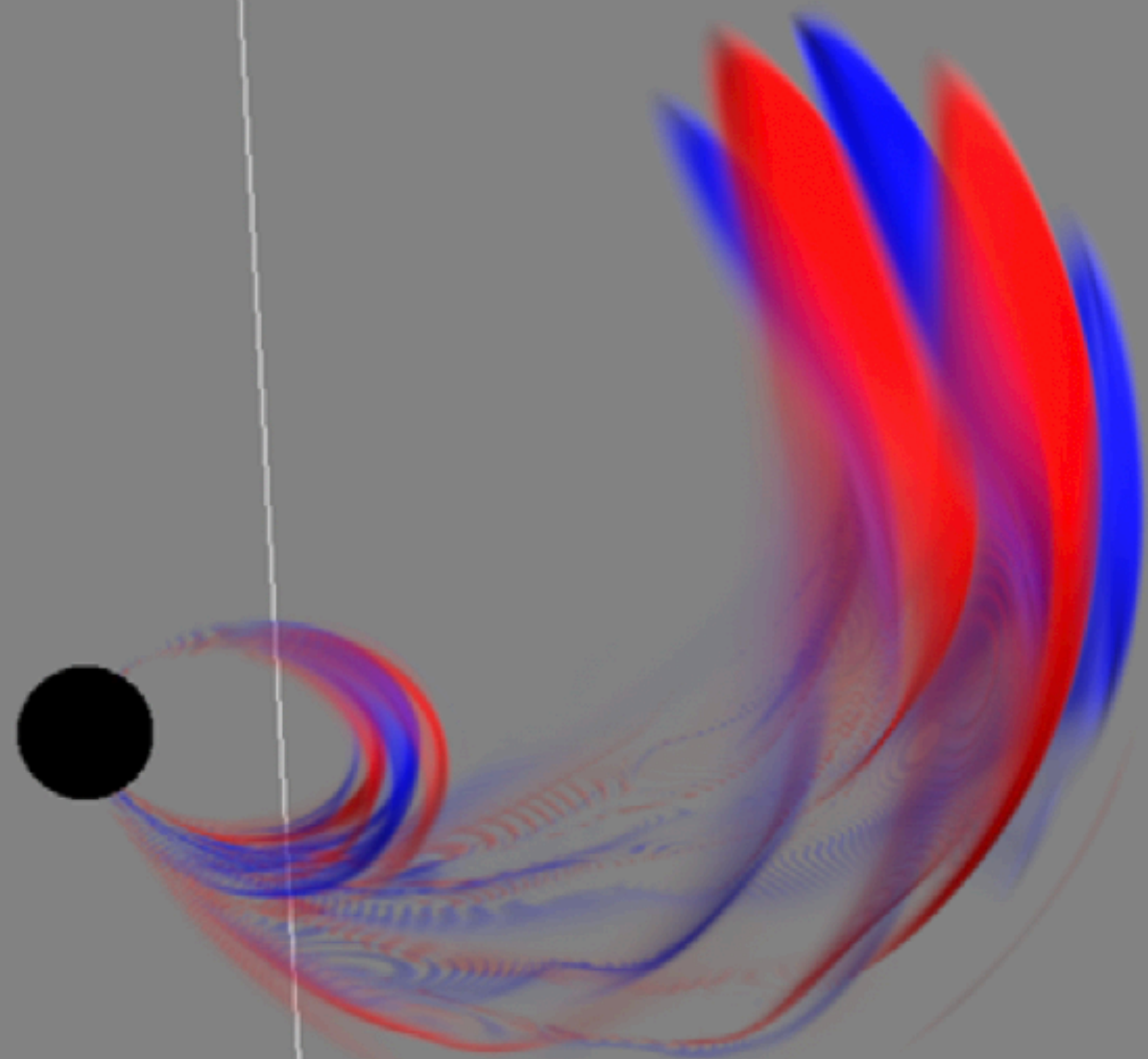
=> energy lost by the kHz wave is
radiated in the X-ray band

II. Alfven waves from quakes

Alfven wave from a quake



$t=20.0$



10^{-8}
-0.250 9.56 19.4 29.2
x

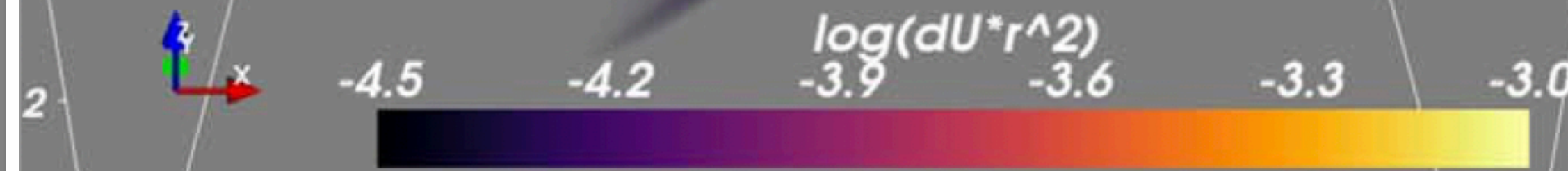
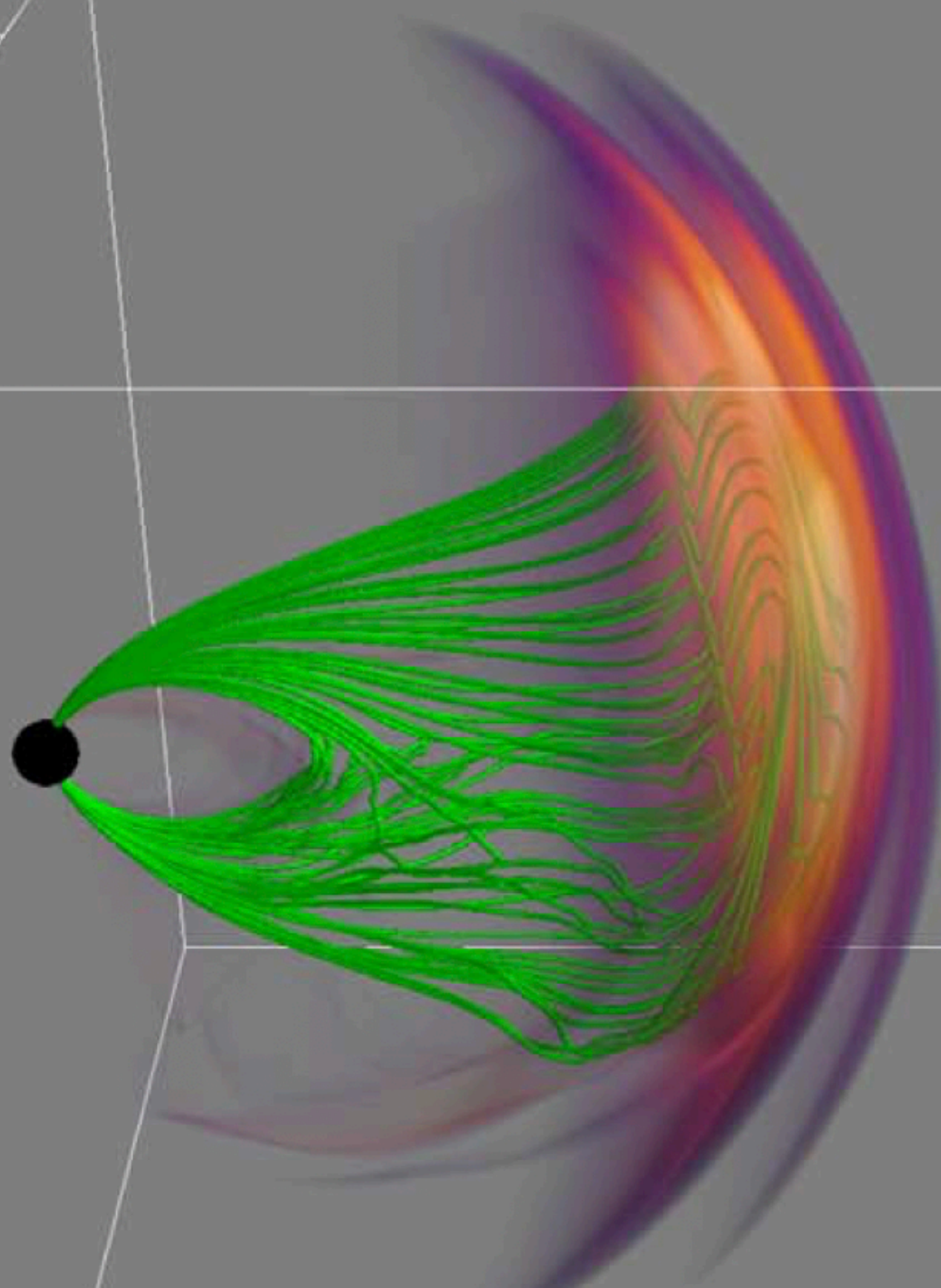


$B_{\phi} \cdot r$
-0.02 -0.01 0.00 0.01 0.02



9.88

$t=30.0$

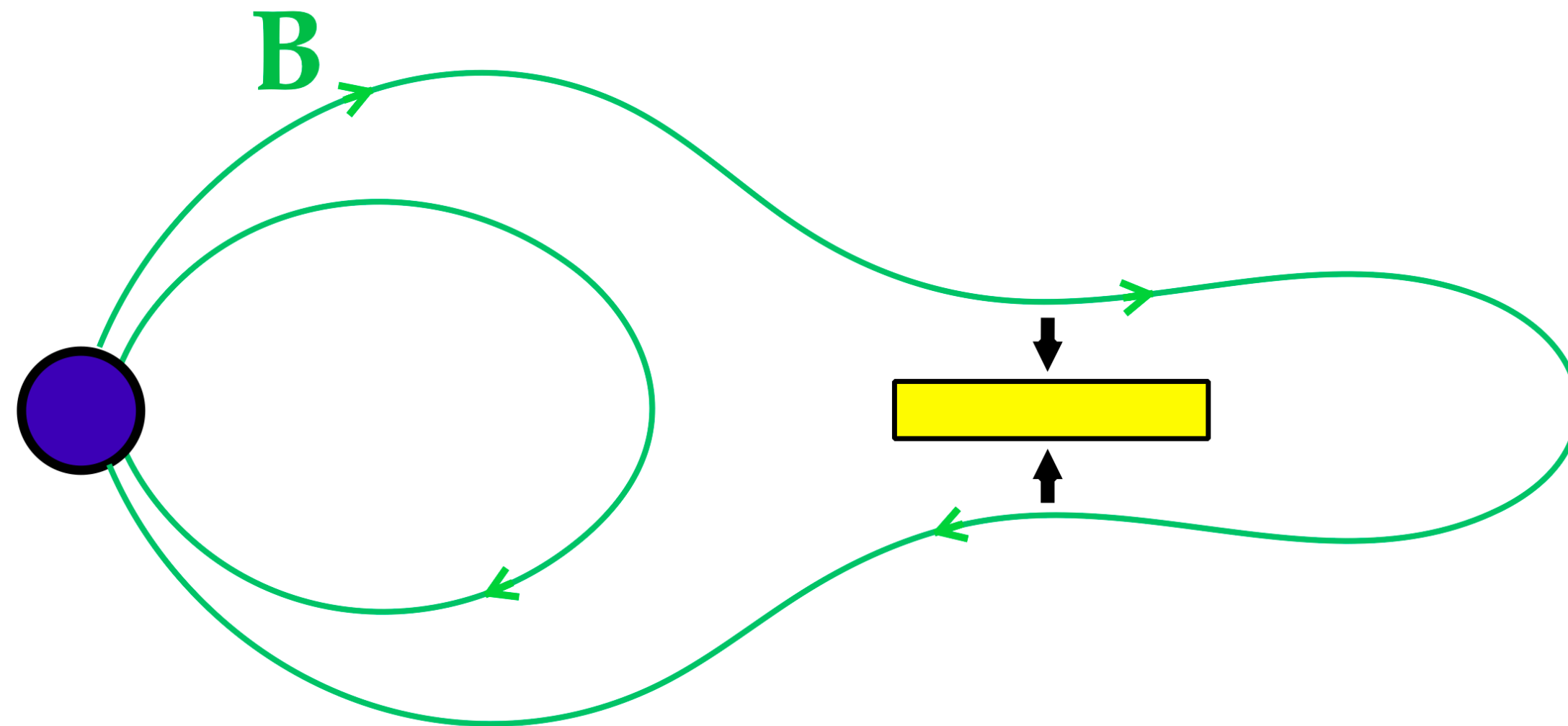


2

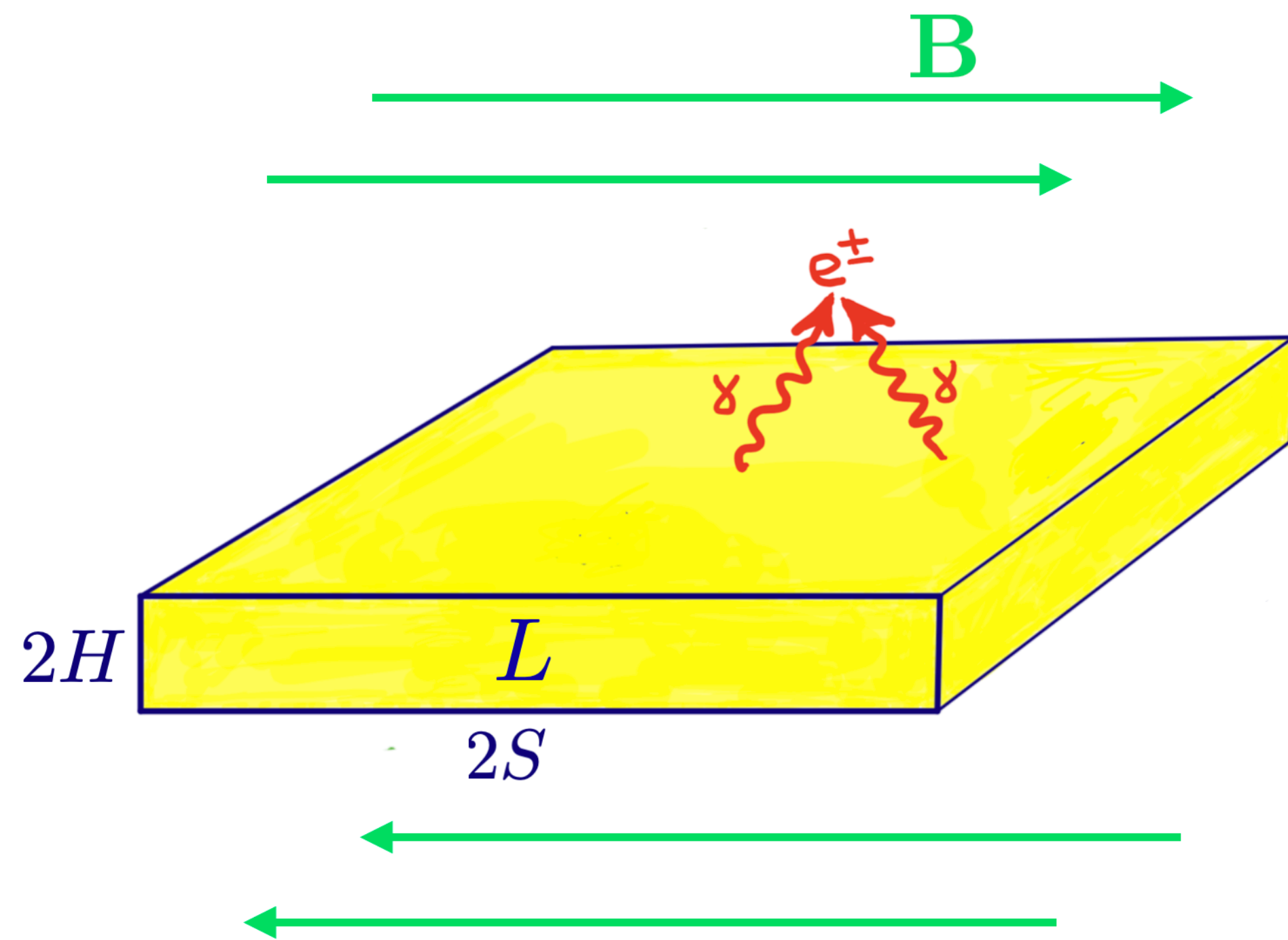


Yuan et al. 2022

Magnetic reconnection

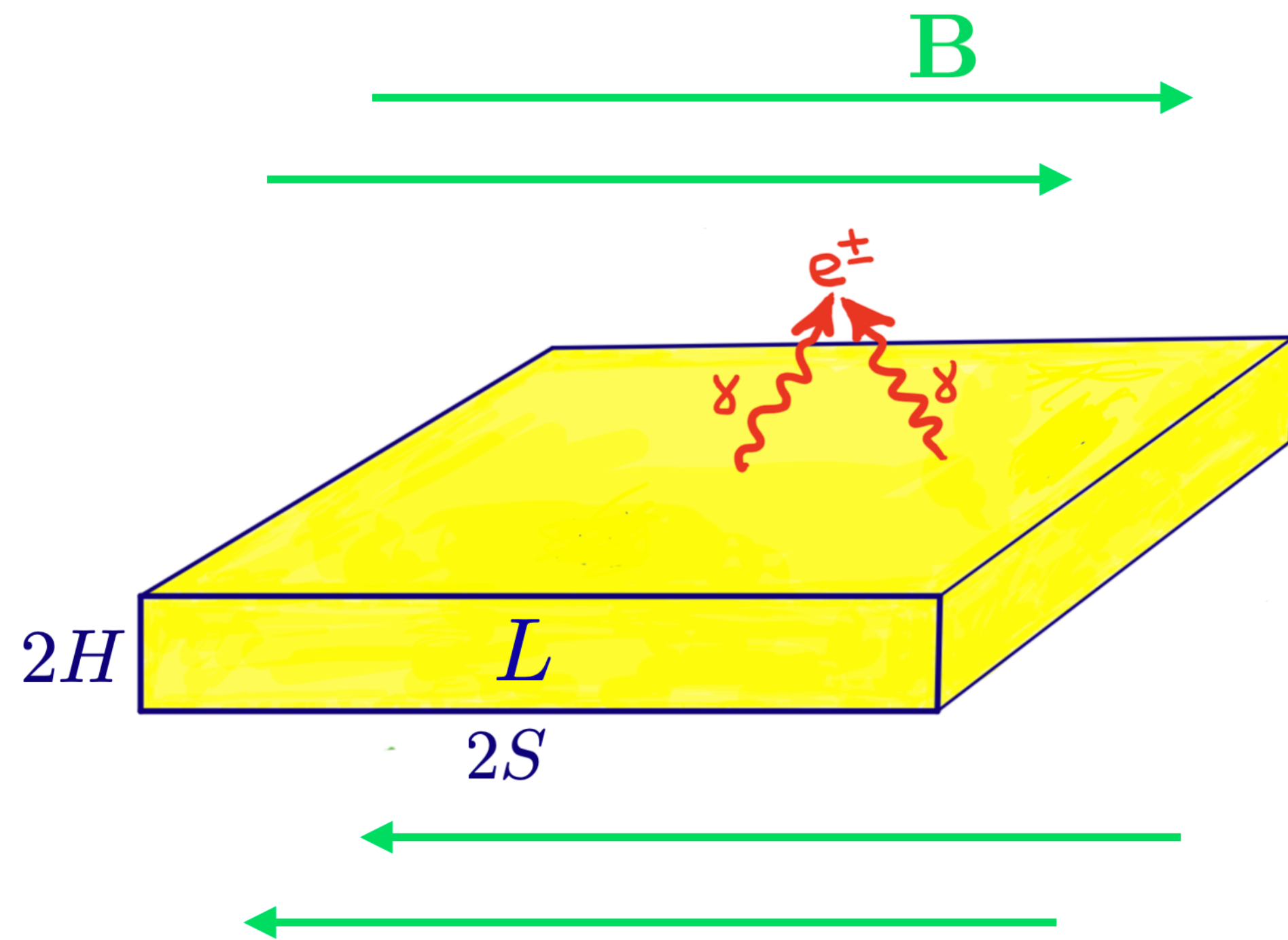


Creation of e^+e^- plasma and X-ray bursts

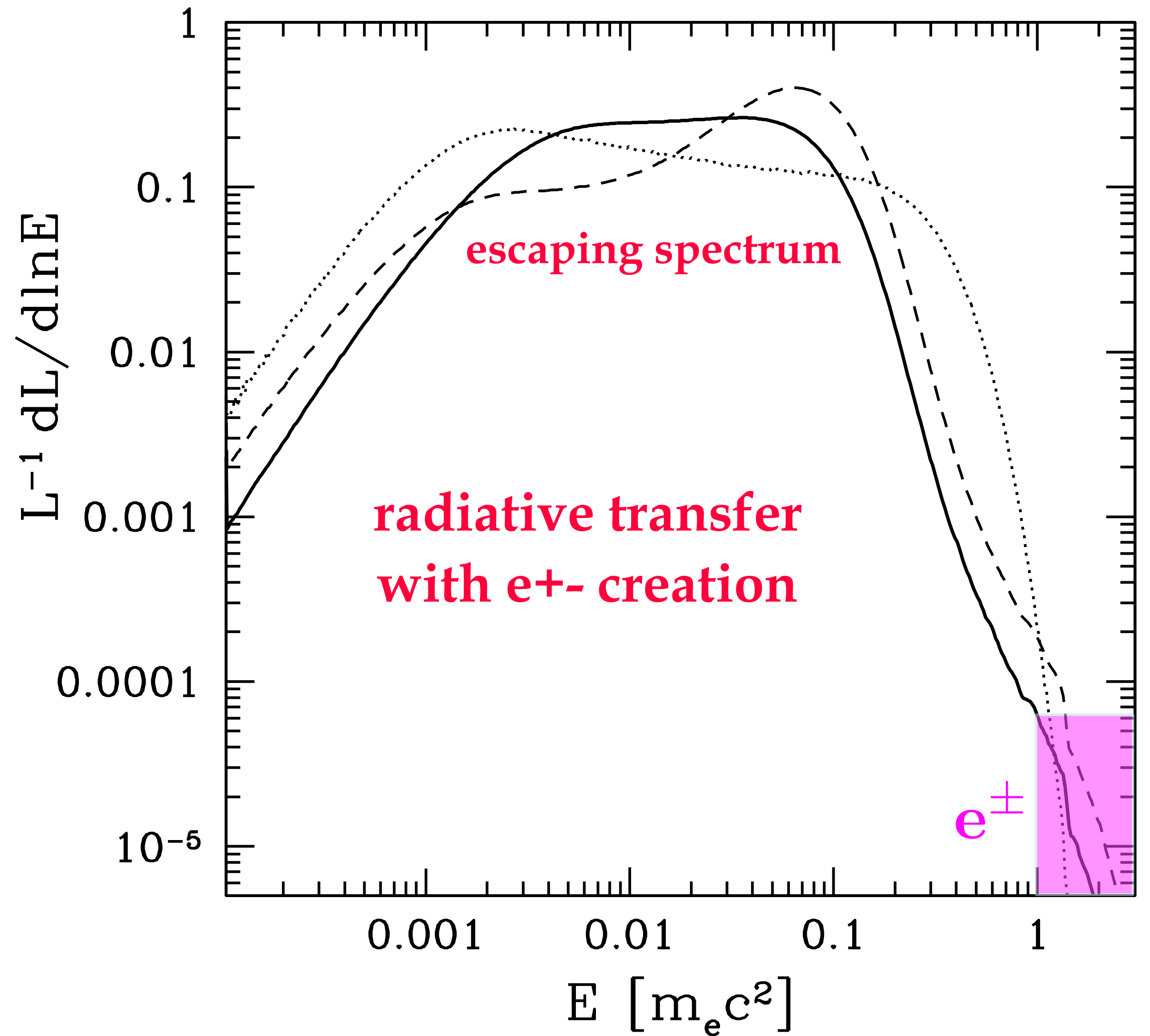


$$\ell_B \equiv \frac{U_B}{m_e c^2} \sigma_T S \approx 3 \times 10^5 B_9^2 S_7$$

Creation of e⁺- plasma and X-ray bursts



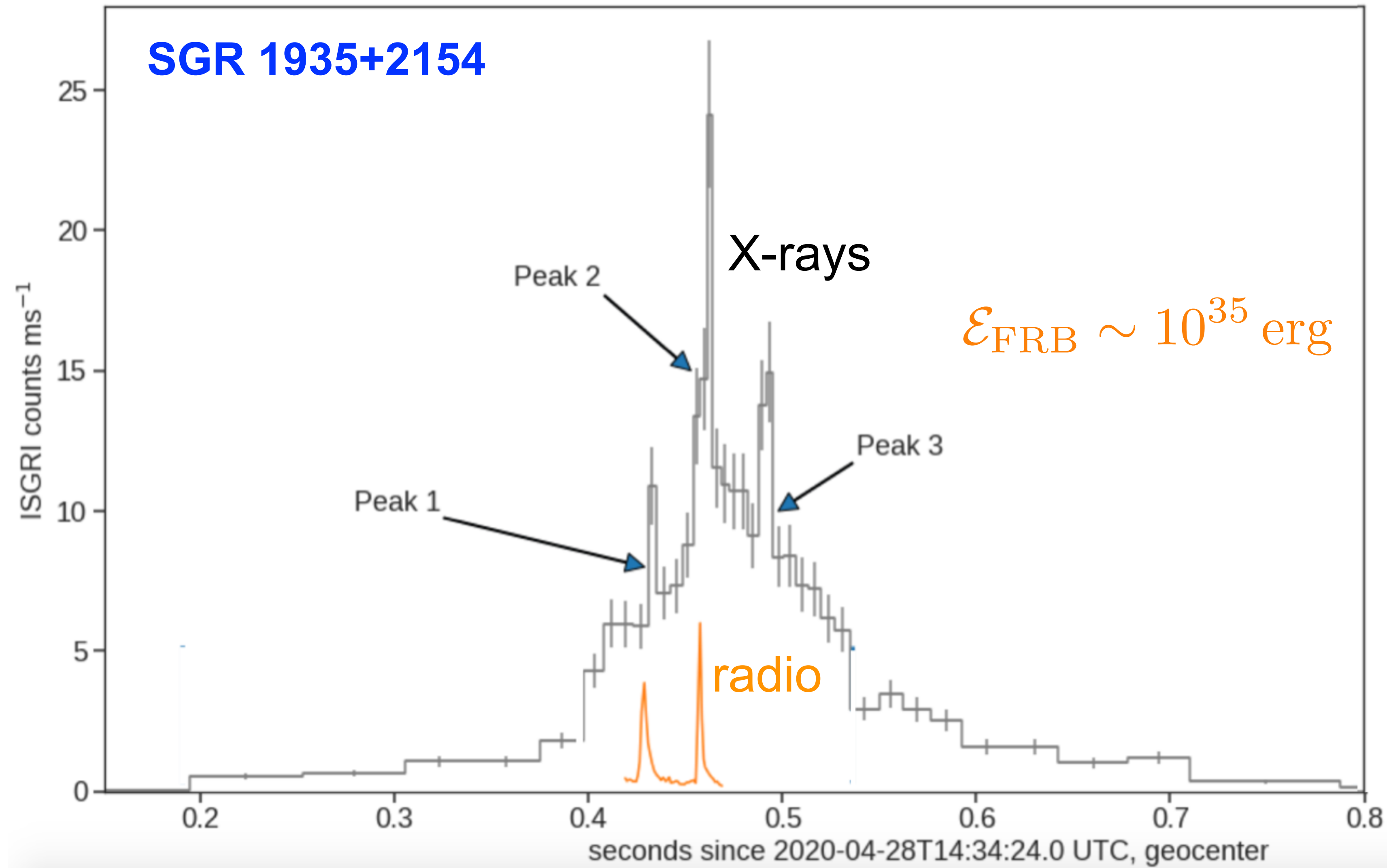
$$\ell_B \equiv \frac{U_B}{m_e c^2} \sigma_T S \approx 3 \times 10^5 B_9^2 S_7$$



$$\frac{n_\pm}{n_\gamma} \sim 10^{-5}$$

$$\frac{kT}{m_e c^2} \sim 0.1$$

April 2020: FRB detection from a local magnetar



FRBs:

- GHz band, ms duration
- detected in distant galaxies
- luminosities up to 10^{43} erg/s

Radio bursts are damped in a static background magnetosphere

=> FRBs must be emitted by magnetic explosions
(and released far from the star, in the wind)

AB 2021, 2023

Golbreikh, Lyubarsky 2023

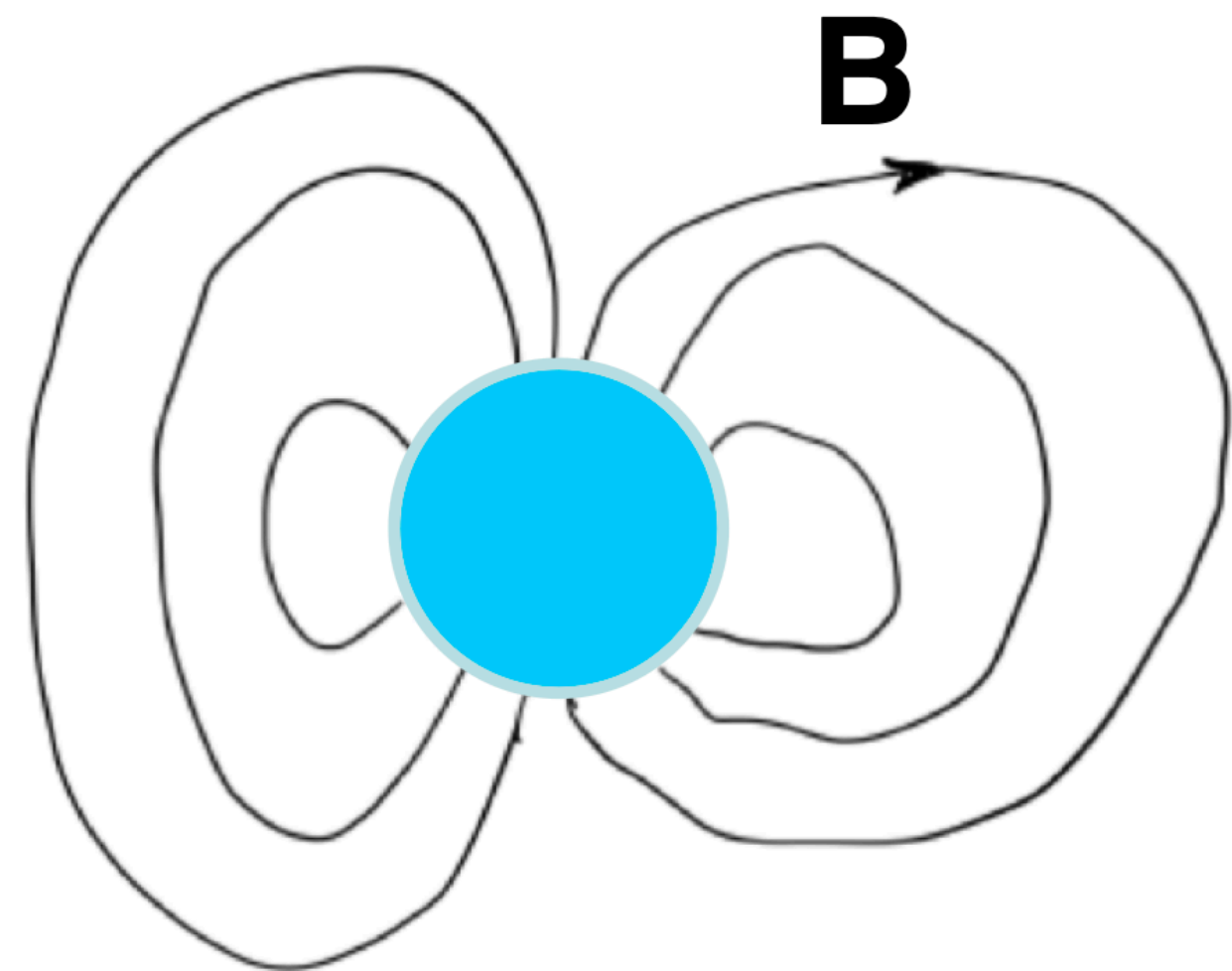
FRB mechanism: magnetic explosion

– shocks in the magnetar wind

AB 2017, 2020;
Metzger et al. 2019

– ejecta carrying waves from magnetic reconnection

Lyubarsky 2020;
Mahlmann et al. 2022



pre-explosion
magnetar
wind
 $\Gamma_w = 10 - 50$

$$\Delta t \approx \frac{r}{c} \left(1 - \frac{v}{c} \right) \approx \frac{r}{2\gamma^2 c}$$



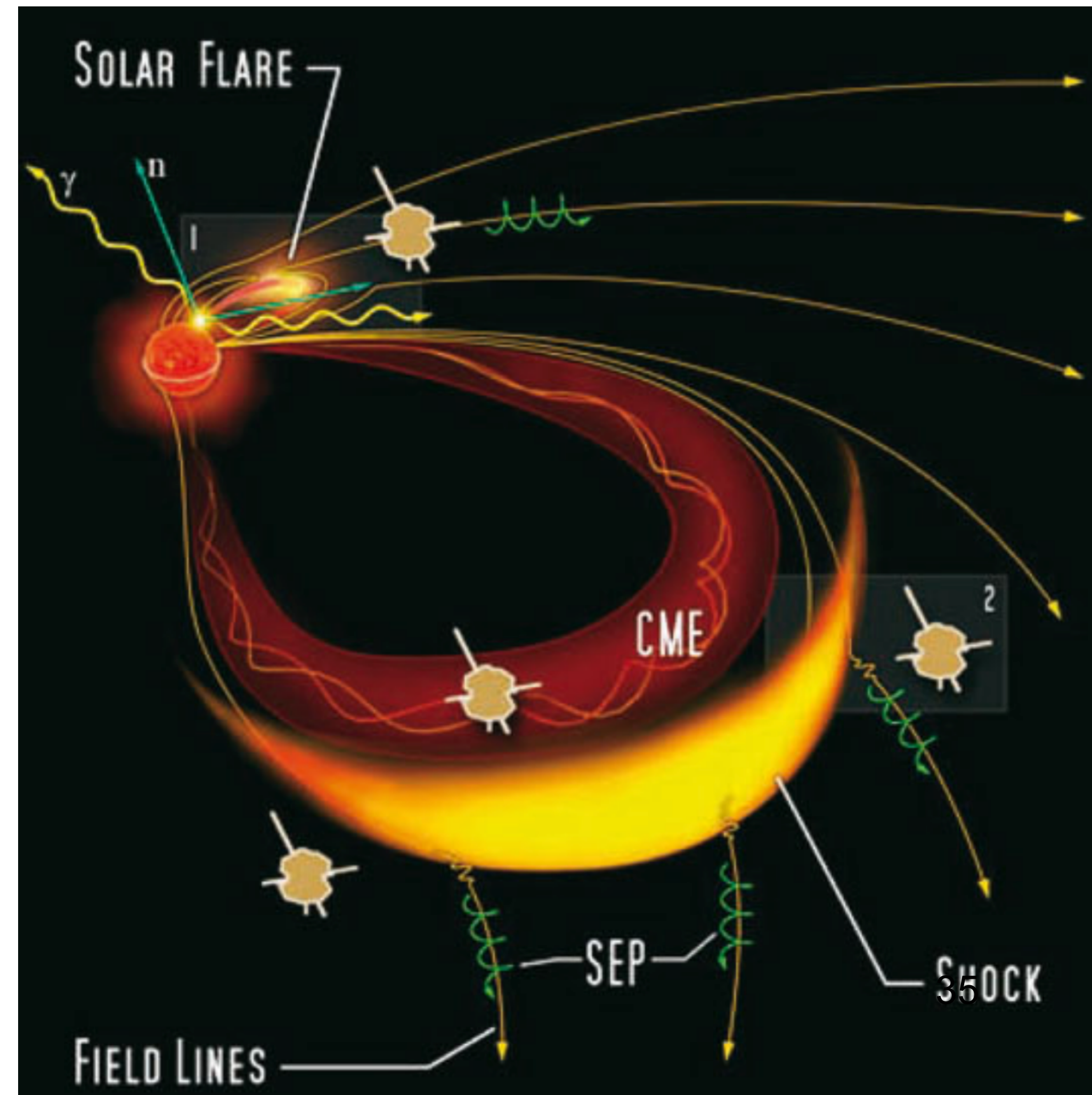
Blast waves from magnetar flares

(cf. solar flares)

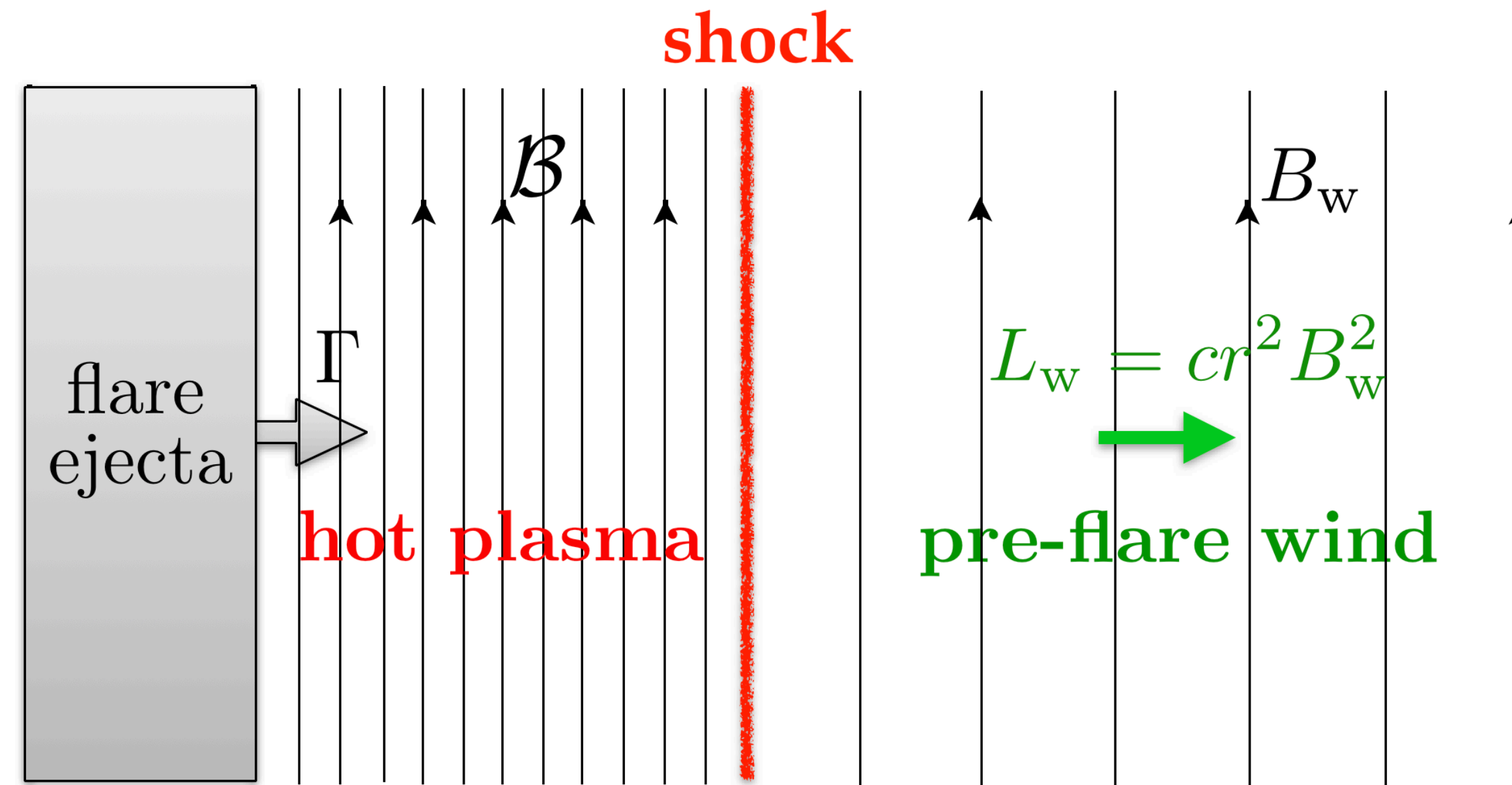
blast Lorentz factor

$$\frac{\Gamma}{\Gamma_w} \approx 100 \left(\frac{L_{f,47}}{L_{w,39}} \right)^{1/4}$$

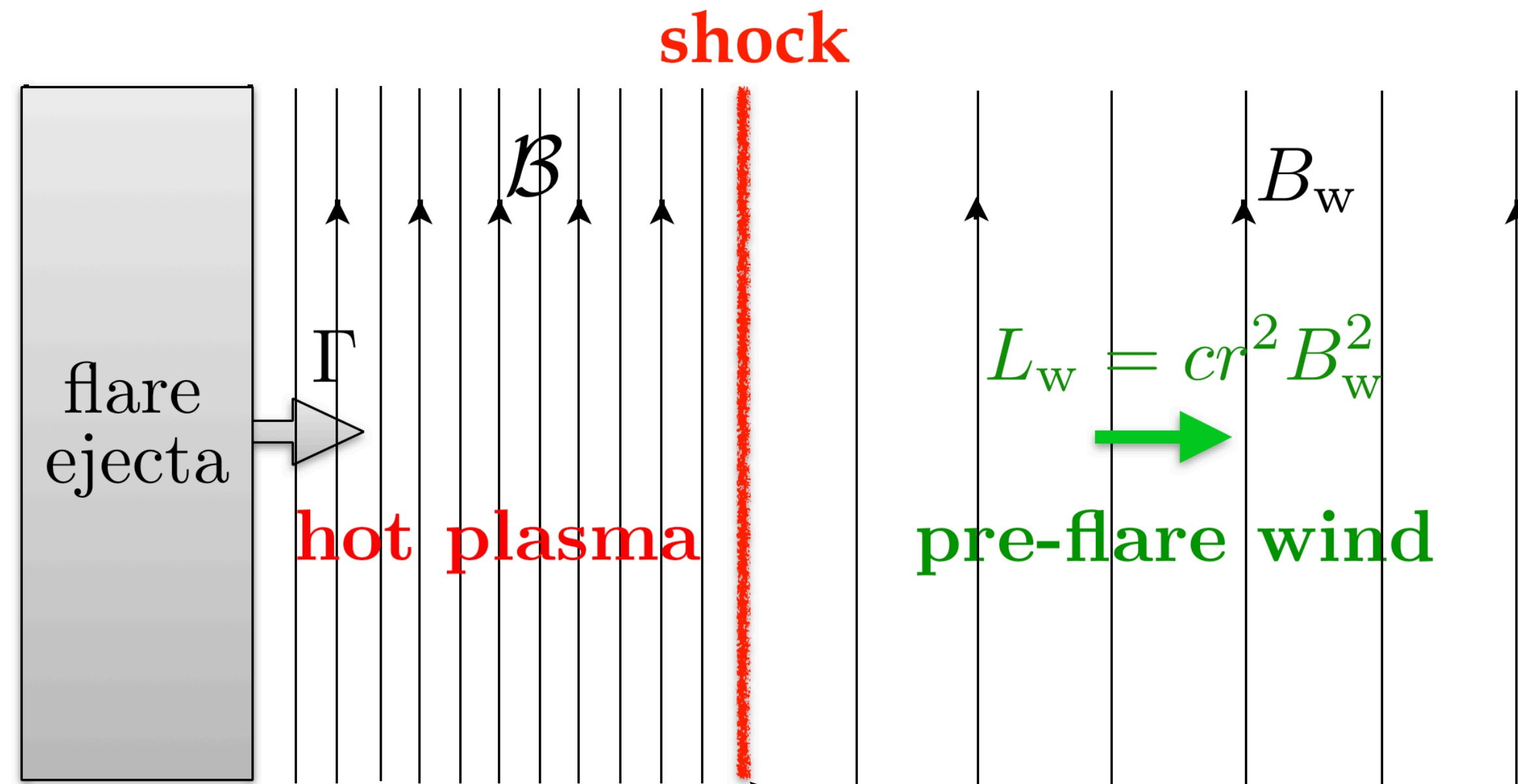
pre-shock wind Lorentz factor



Coherent emission mechanism: shock maser

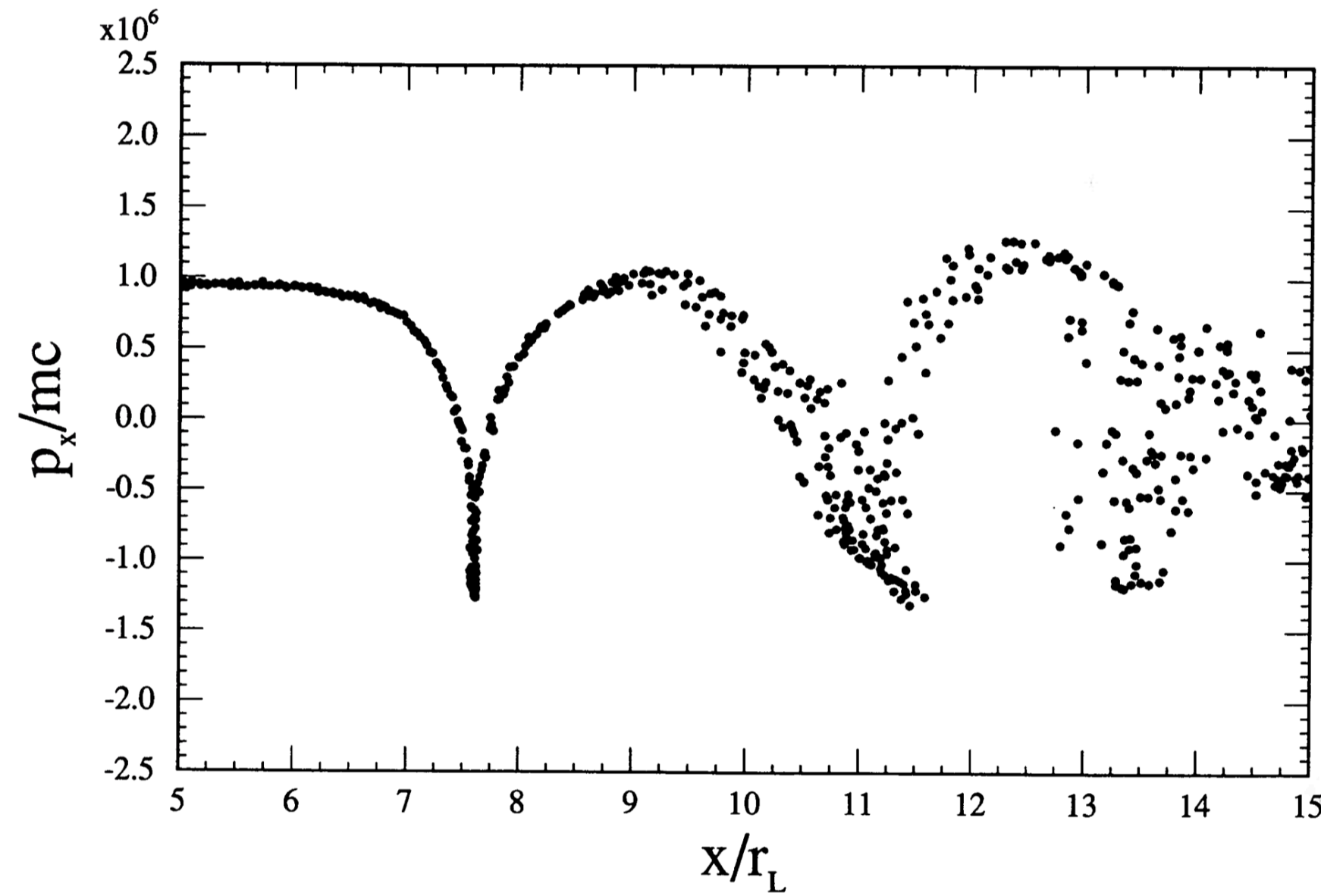


Coherent emission mechanism: shock maser



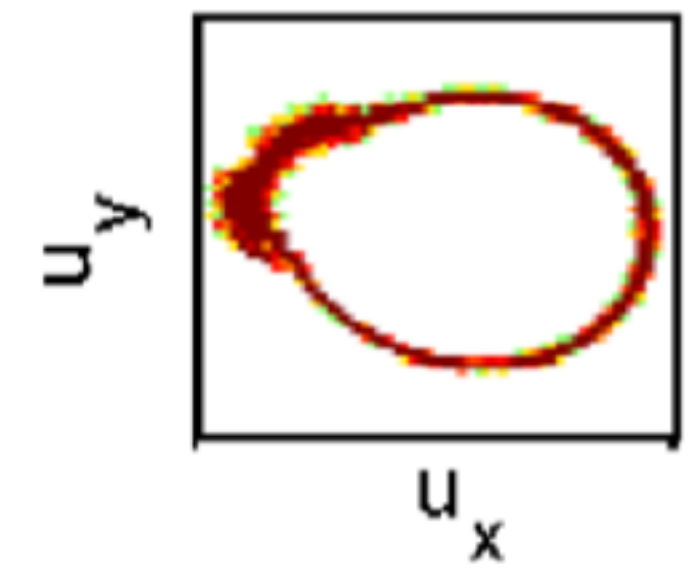
maser: Larmor rotation

$$r_L = \frac{\Gamma_{\text{rel}} m_e c^2}{eB}$$

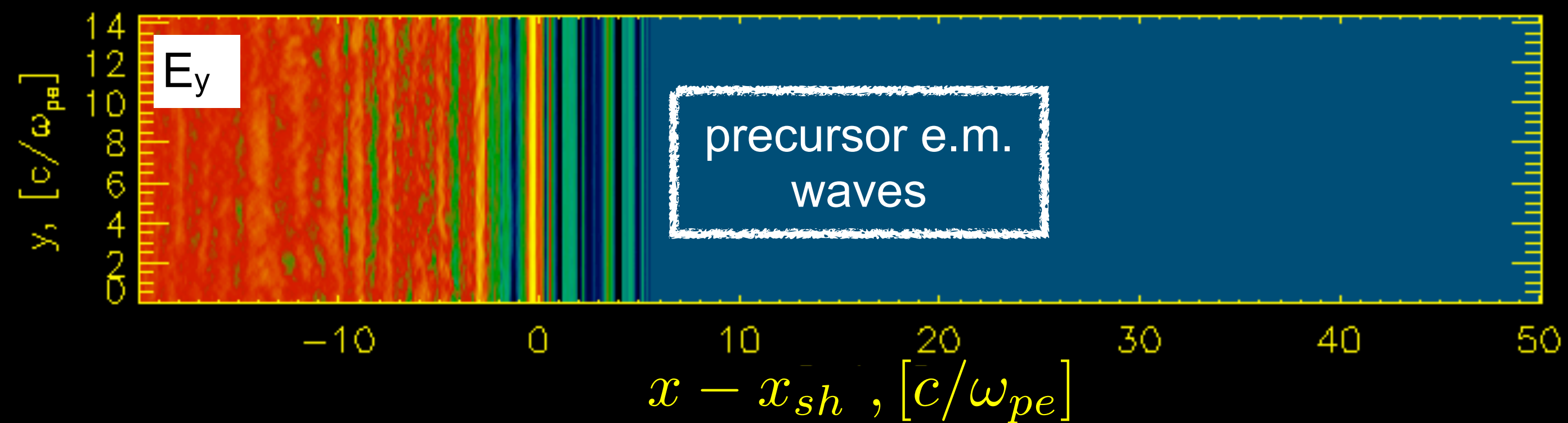
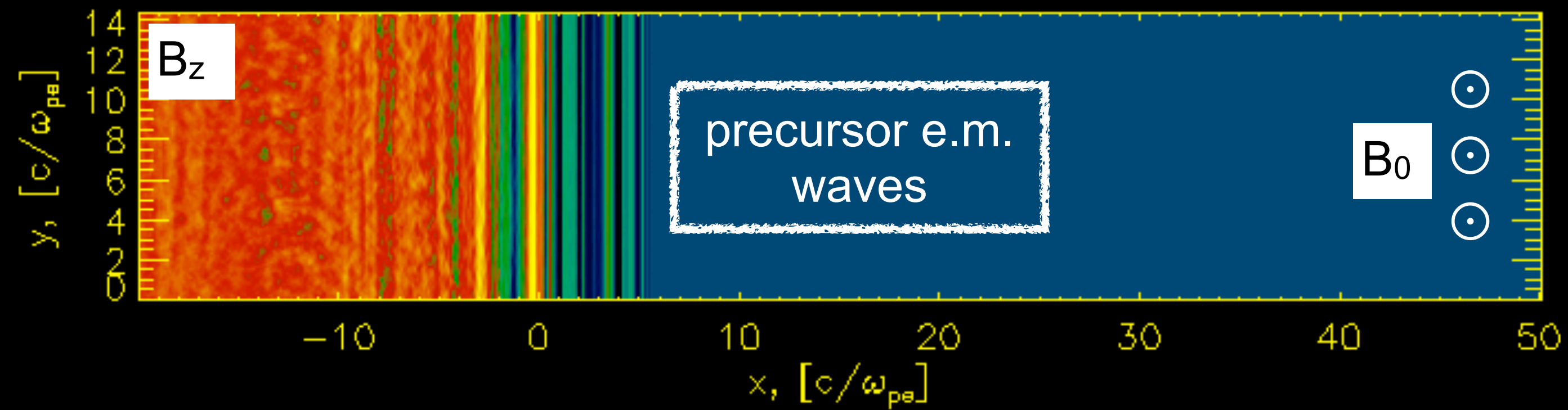
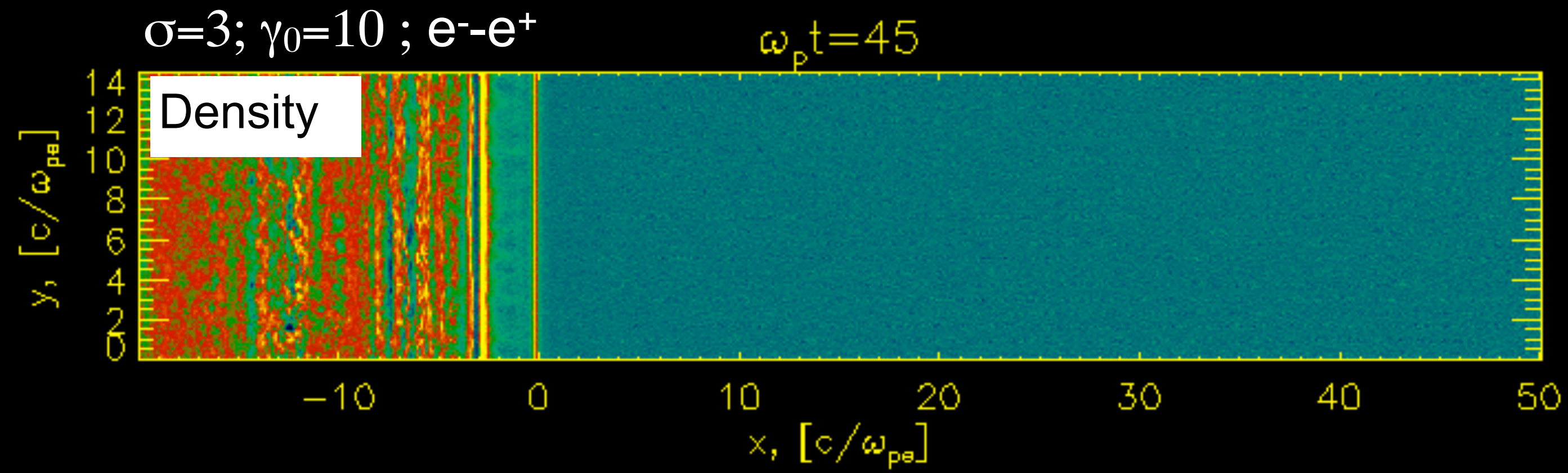


Kinetic simulations:

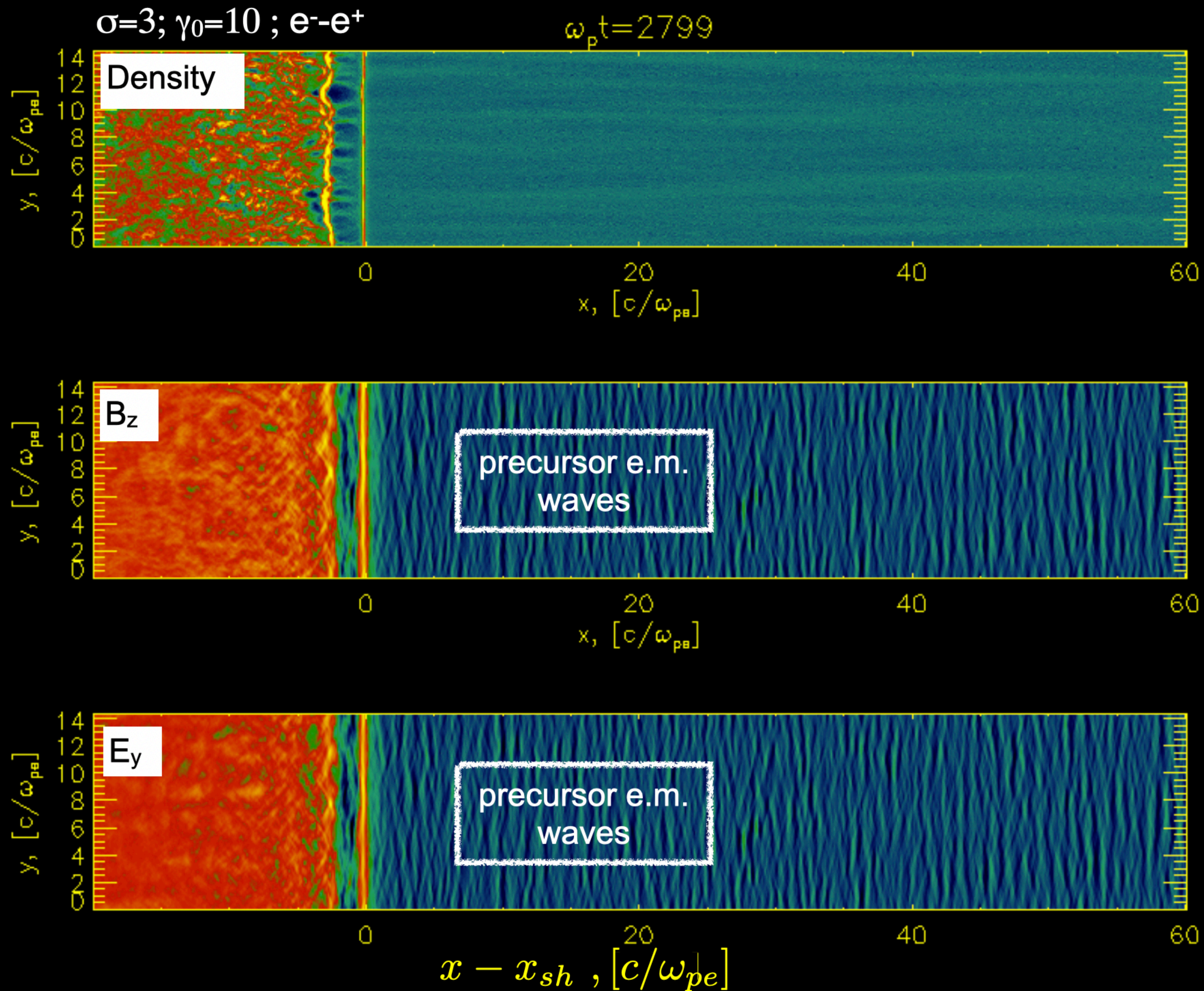
- Gallant et al. 1992
- Iwamoto et al. 2017, 2018
- Plotnikov & Sironi 2019
- Sironi et al. 2021



Shock-powered coherent emission



Shock-powered coherent emission



Summary: ejecta and bursts from magnetars

perturbations
(quakes) \rightarrow $\left[\begin{array}{l} \text{monster radiative shocks} \\ \text{nonlinear Alfvén waves} \end{array} \right] \rightarrow$ ultra-relativistic
explosions
 $(R \sim 100R_*)$

(plasma acceleration to Lorentz factors exceeding 10^6)

production of radiation: X-ray bursts ($R \sim 100R_*$)

FRBs (when ejecta expand far beyond
the magnetosphere, $R \sim 1\text{AU}$)